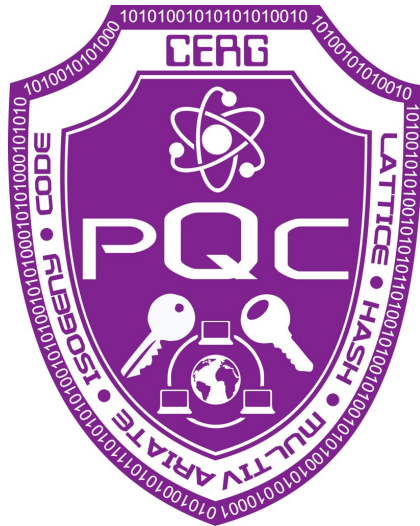


Post-Quantum Cryptography Standardization, As Driven by NIST, Summarized

Kris Gaj



Thank You!

Great thanks to

Prof. Bertrand Cambou

& the entire VICEROY Symposium Organizing Committee

for the kind invitation
to give this talk!

CERG: Cryptographic Engineering Research Group



- 3 faculty members
- 7 Ph.D. students
- 5 MS students
- 10 affiliated scholars

Recent and Current CERG Group Members supporting PQC

Recent Graduates



Farnoud

SW/HW Codesign
RTL Accelerators

Experimental Setup for
Timing Measurements
CAD Tools

Apple



Bakry

Experimental Setup
for Side-Channel
Analysis

Lightweight
Architectures

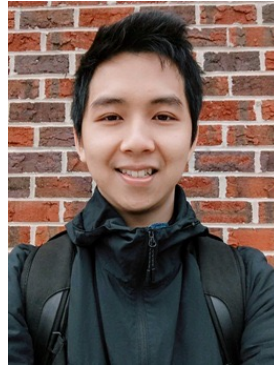
PQSecure



Viet

RTL Design of
HW Accelerators
for Lattice-based
& Code-based PQC

Qualcomm



Duc

HLS Design of
HW Accelerators
for Lattice-based
PQC

NEON-based SW
implementations



Kamyar

RTL Design of
HW Accelerators
for Lattice-based
PQC

Side-Channel
Analysis

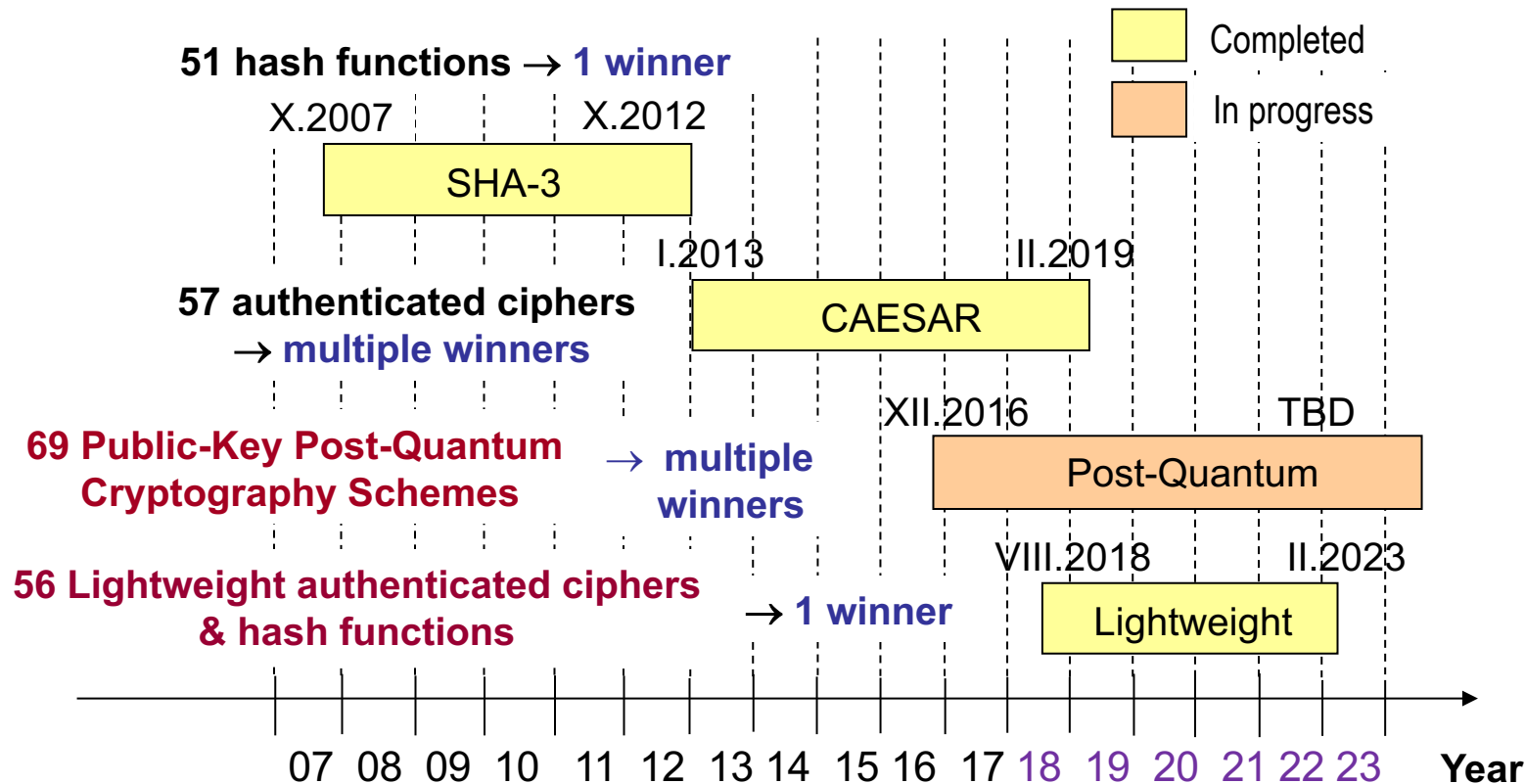


Luke

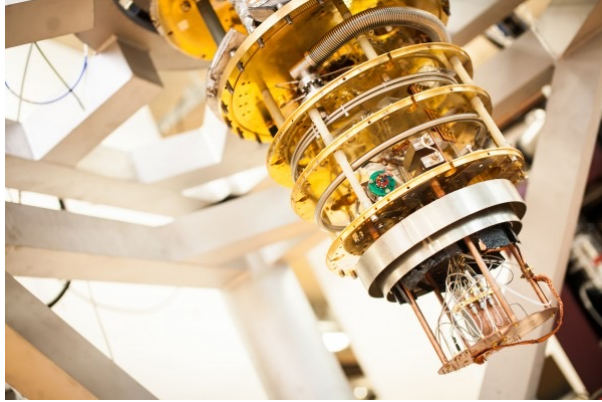
RTL Design of
HW Accelerators
for Lattice-based
PQC

Power & Energy
Measurements

CERG Participation in Cryptographic Contests 2007-Present



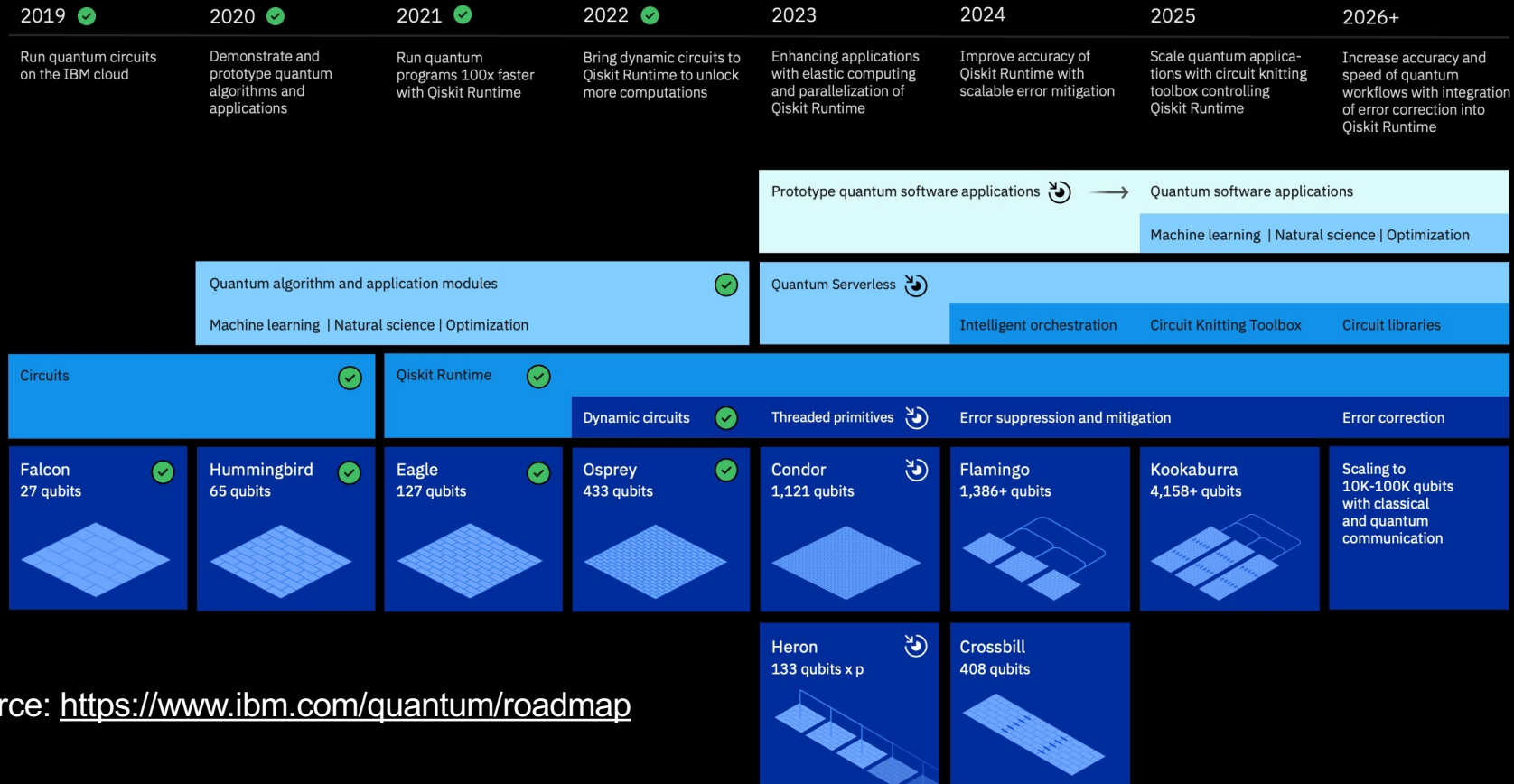
Quantum Computers



- Substantial investments by: Google, IBM, Intel, Microsoft, and governments of multiple countries

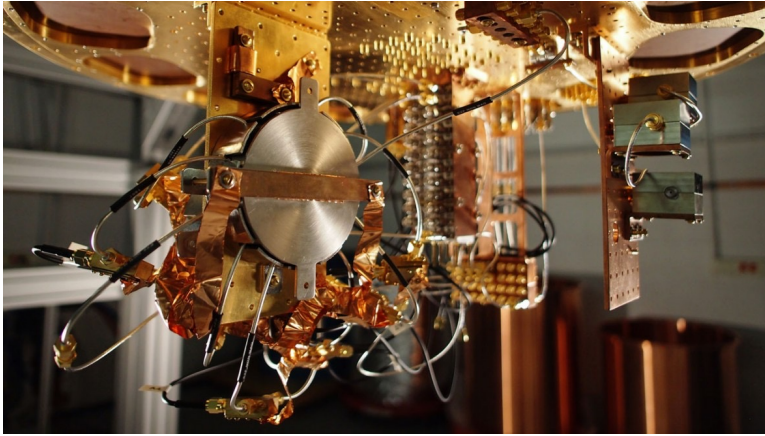


- Jan 2018: Intel's 49-qubit "Tangle Lake" processor
- Mar 2018: Google's 72-qubit "Bristlecone" processor
- 2020-2021: Three quantum computers developed at the University of Science and Technology of China reach quantum supremacy
- Nov 2022: IBM's 433-qubit "Osprey" processor

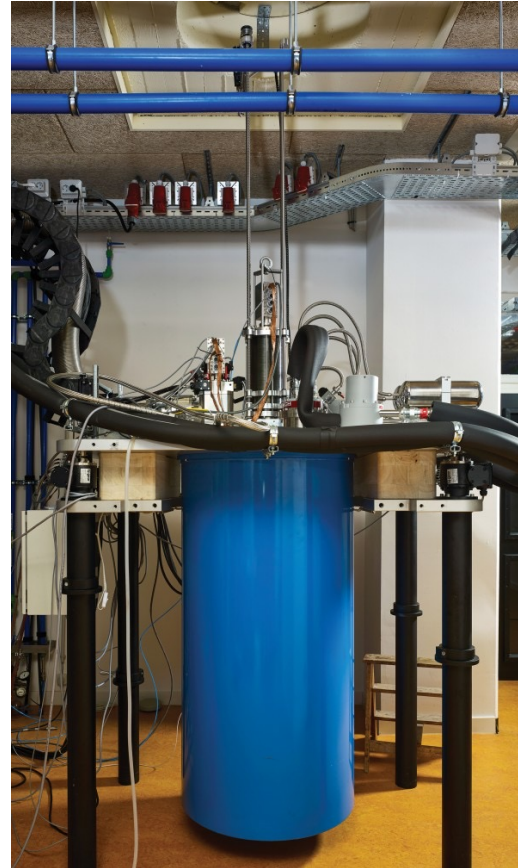


Source: <https://www.ibm.com/quantum/roadmap>

Progress in Quantum Computing



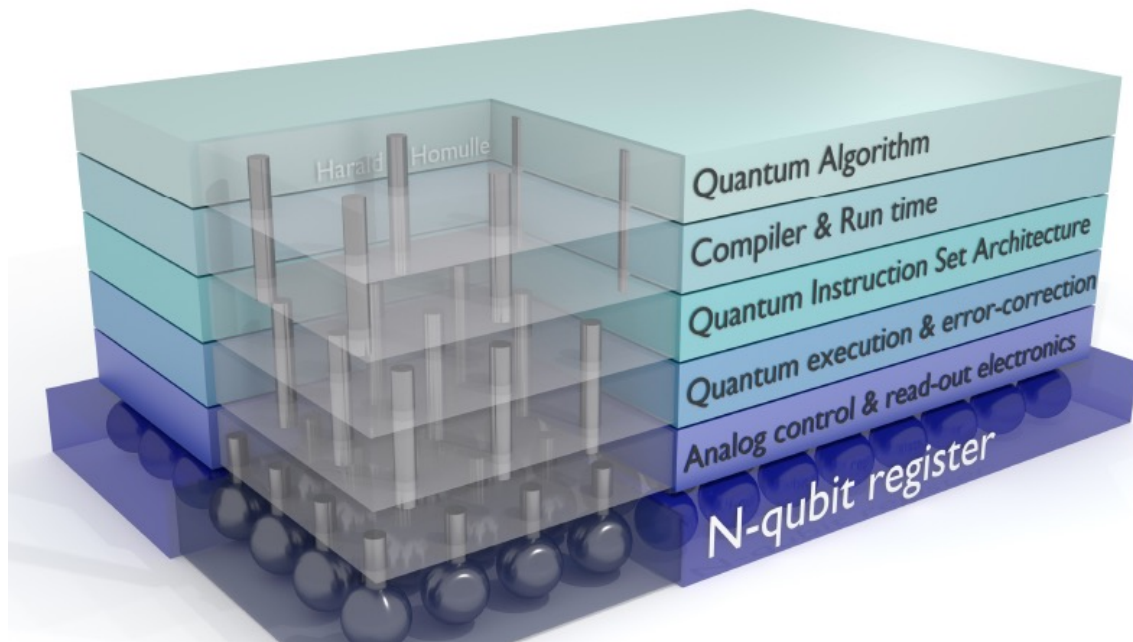
Google and IBM quantum computers based on superconducting circuits operating in the temperature close to absolute 0 (~ 0.01 K)



System Layer Approach

Challenges in each layer

Layers are highly interrelated



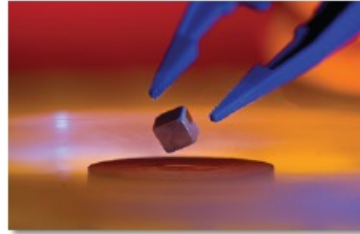
What Quantum Computers Can Do?

Model complex molecules



Health: Quantum chemistry for medicine

Model complex materials



Energy: Room-temperature superconductivity

Solve complex math problems



Security: factoring and code breaking

Nobel 2012 citation: *“The quantum computer may **change our everyday lives** in this century in the same radical way as the classical computer did in the last century.”*

Best known attack using quantum computers

1996: **Grover's Algorithm**, reduces the time of the exhaustive-key search for secret key ciphers

from 2^k to $2^{k/2}$ operations, for a k -bit key,
e.g., from 2^{128} to 2^{64} operations, for a 128-bit key or
from 2^{256} to 2^{128} operations, for a 256-bit key

assuming
a sufficiently powerful and reliable quantum computer available

Easy Countermeasure: Double the size of a key

Effect on Public-Key Cryptography

1994: **Shor's Algorithm**, breaks major public key cryptosystems based on

Factoring:

RSA

Discrete logarithm problem (DLP): DSA, Diffie-Hellman

Elliptic Curve DLP:

Elliptic Curve Cryptosystems

independently of the key size

assuming

a sufficiently powerful and reliable quantum computer available

Bases of the traditional public cryptosystems security

	Factorization	Discrete Logarithm	Elliptic Curve Discrete Logarithm
Given:	$N = p \cdot q$	$y = g^x \text{ mod } p =$ $= \underbrace{g \cdot g \cdot g \cdot \dots \cdot g}_{x \text{ times}}$ <p>constants p, g</p>	$Q = x \cdot P =$ $= \underbrace{P + P + \dots + P}_{x \text{ times}}$ <p>P - point of an elliptic curve</p>
Unknown:	p, q	x	x

Underlying Mathematical Problem - RSA

$$N = P * Q \text{ (P, Q random primes)}$$

214032465024074496126442307283933356300861471514475501779775492
088141802344714013664334551909580467961099285187247091458768739
626192155736304745477052080511905649310668769159001975940569345
7452230589325976697471681738069364894699871578494975937497937

=

641352894770715802787901901705773890848250147429434472081168596
32024532344630238623598752668347708737661925585694639798853367

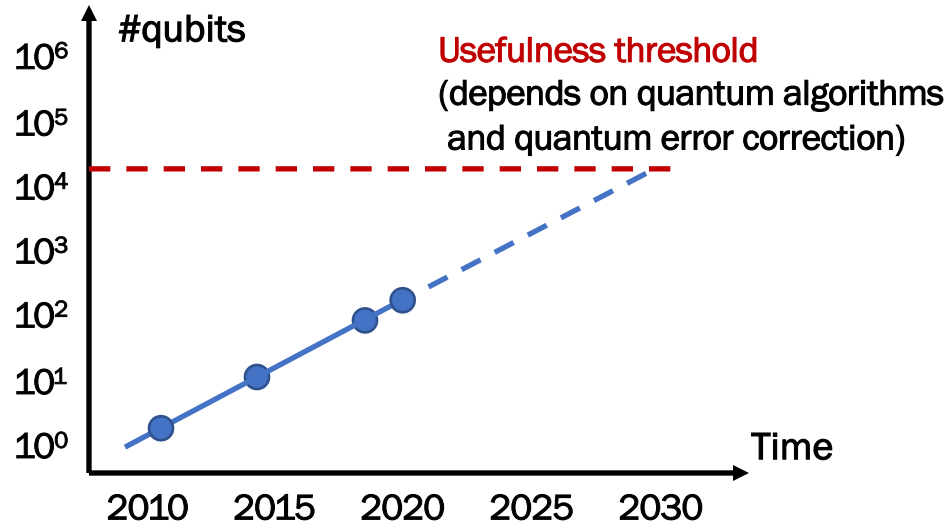
*

333720275949781565562260106053551142279407603447675546667845209
87023841729210037080257448673296881877565718986258036932062711

Record Using Classical Computers, 250 decimal digits, 829 bits

Announced on February 28, 2020

How Real Is the Danger?



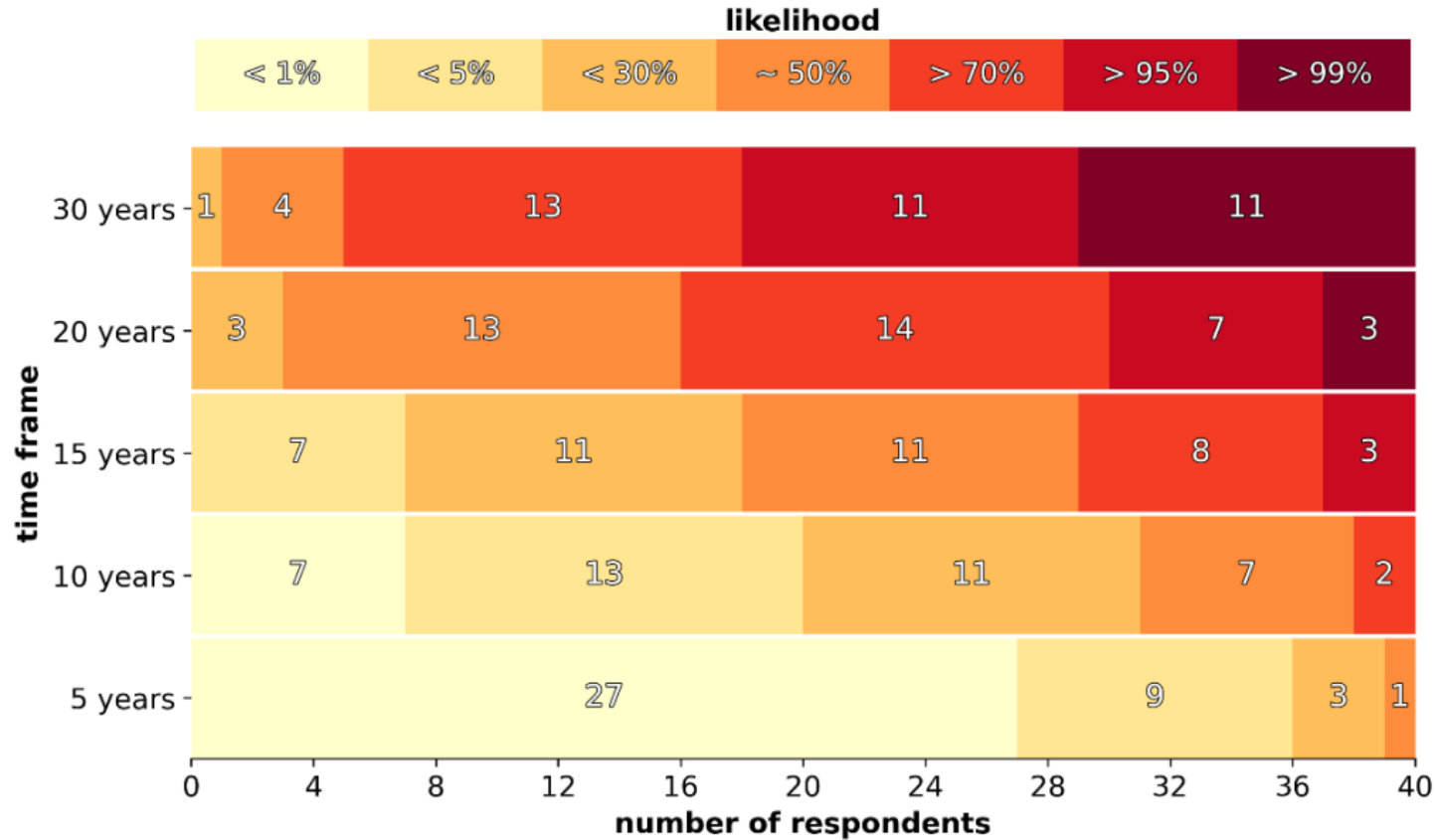
“There is a 1 in 5 chance that some fundamental public-key crypto will be broken by quantum by 2029.”

Dr. Michele Mosca

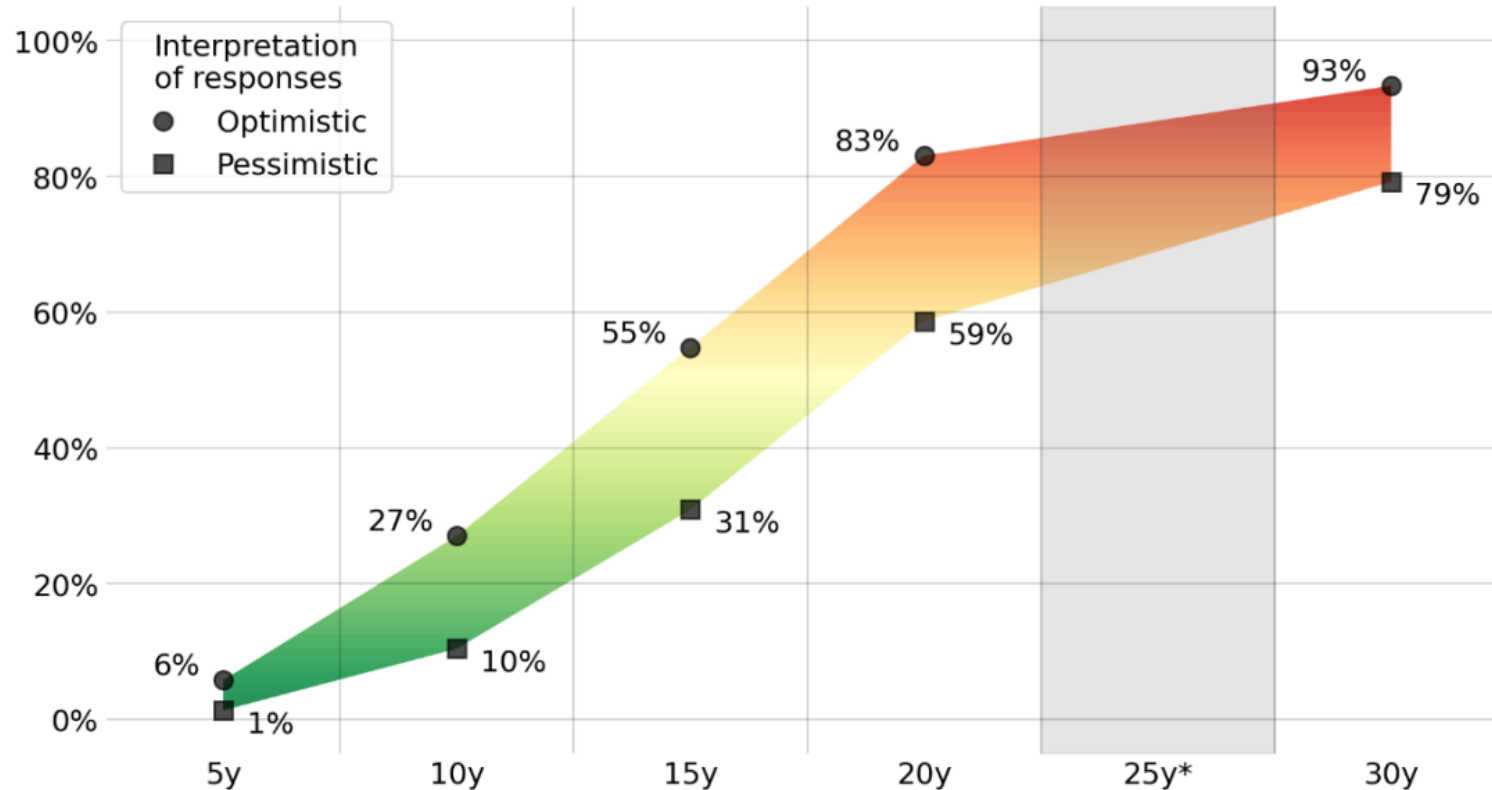
Deputy Director of the Institute for Quantum Computing, University of Waterloo

2020

2022 Experts' Estimates of Likelihood of a Quantum Computer Able to Break RSA-2048 in 24 hours



2022 Opinion-Based Estimates of the Probability of a Quantum Computer Being Able to Break RSA-2048 in 24 hours



“Theorem” by Mosca

If $z < y + x$, then worry!



Encrypted Data Stored by Powerful
Adversaries

No Announcement when Quantum Computer
Available to NSA, Foreign Governments,
or Organized Crime

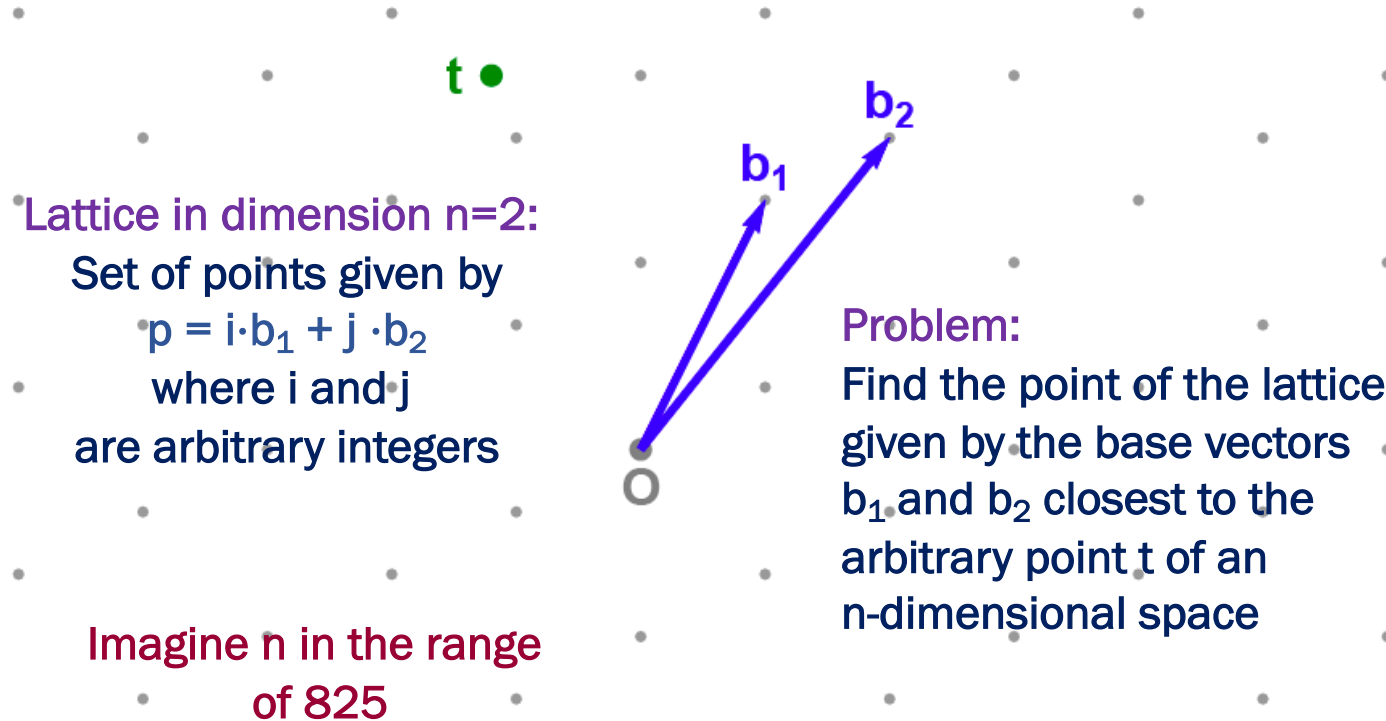
Post-Quantum Cryptography (PQC)

- Public-key cryptographic algorithms for which there are **no known attacks** using quantum computers
 - Capable of being implemented using any **traditional** methods, including **software and hardware**
 - Running efficiently on **any modern computing platforms**: PCs, tablets, smartphones, servers with FPGA accelerators, etc.
- Based entirely on traditional semiconductor VLSI technology!

The biggest revolution in cryptography, since the invention of public-key cryptography in 1970s!!!

Underlying Mathematical Problem – Lattice-Based PQC

Closest Vector Problem



Underlying Mathematical Problem – Multivariate PQC

Solving a system of m quadratic equations with n unknowns

$$p^{(1)}(x_1, \dots, x_n) = \sum_{i=1}^n \sum_{j=i}^n p_{ij}^{(1)} \cdot x_i x_j + \sum_{i=1}^n p_i^{(1)} \cdot x_i \left(+ p_0^{(1)} \right)$$

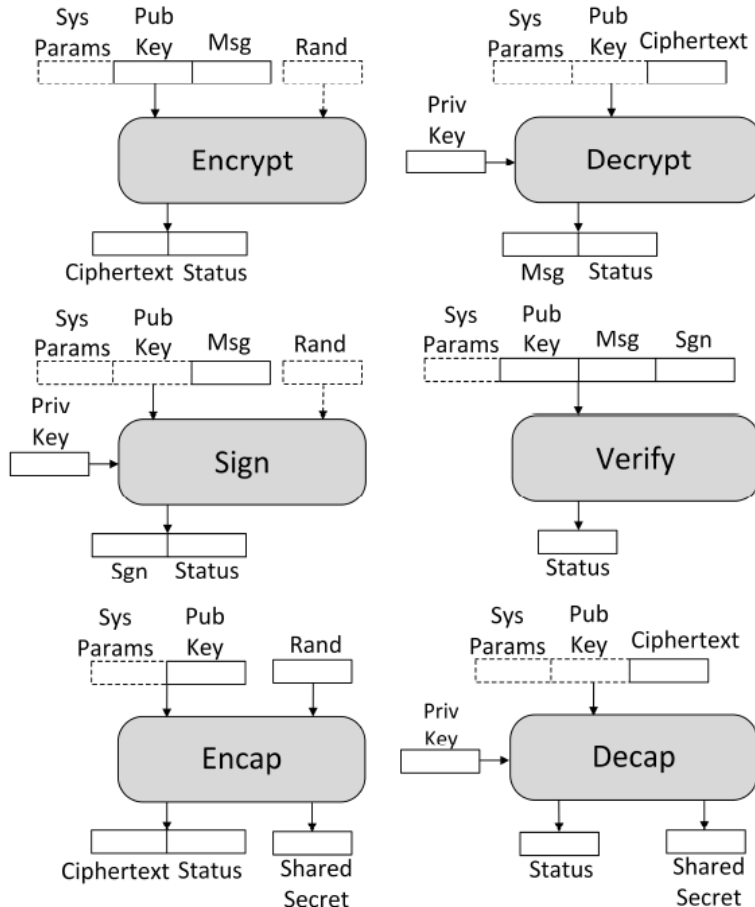
$$p^{(2)}(x_1, \dots, x_n) = \sum_{i=1}^n \sum_{j=i}^n p_{ij}^{(2)} \cdot x_i x_j + \sum_{i=1}^n p_i^{(2)} \cdot x_i \left(+ p_0^{(2)} \right)$$

\vdots

$$p^{(m)}(x_1, \dots, x_n) = \sum_{i=1}^n \sum_{j=i}^n p_{ij}^{(m)} \cdot x_i x_j + \sum_{i=1}^n p_i^{(m)} \cdot x_i \left(+ p_0^{(m)} \right)$$

Imagine m and n in the range of 70 and above

Three Types of PQC Schemes



1. Public Key Encryption

2. Digital Signature

3. Key Encapsulation Mechanism (KEM)

Five Security Levels

Level	Security Description
1	At least as hard to break as AES-128 using exhaustive key search
2	At least as hard to break as SHA-256 using collision search
3	At least as hard to break as AES-192 using exhaustive key search
4	At least as hard to break as SHA-384 using collision search
5	At least as hard to break as AES-256 using exhaustive key search

Leading PQC Families

Family	Encryption/ KEM	Signature
Symmetric-based		XX
Code-based	XX	X
Lattice-based	XX	XX
Multivariate	X	XX
Isogeny-based	X	

XX – high-confidence candidates, X – medium-confidence candidates

Two Major Types of Schemes & Corresponding Families

Post-Quantum
Public Key Exchange

Post-Quantum
Digital Signatures

Lattice-based

Code-based

Symmetric-based

Isogeny-based

Multivariate

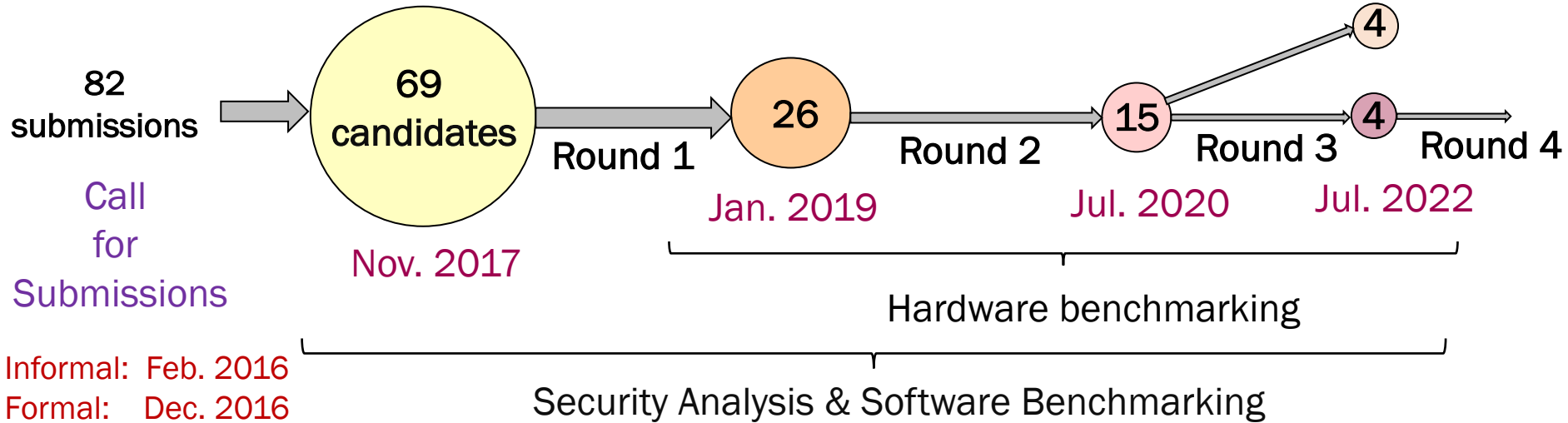
Informal Call for Submissions – PQCrypto 2016

Fukuoka, Japan, February 24-26, 2016



NIST PQC Standardization Process

Near-term standards



Round 1 Submissions as of May 2018



69 Submissions accepted to Round 1, 26 Countries, 278 co-authors

BIG QUAKE. BIKE. **CFPKM**. Classic McEliece. **Compact LWE**. CRYSTALS-DILITHIUM. CRYSTALS-KYBER. DAGS. Ding Key Exchange. **DME**. DRS. DualModeMS. **Edon-K**. EMBLEM and R.EMBLEM. FALCON. FrodoKEM. GeMSS. **Giophantus**. Gravity-SPHINCS. **Guess Again**. Gui. **HILA5**. HiMQ-3. **HK17**. HQC. KINDI. LAC. LAKE. **LEDAkem**. **LEDApkc**. **Lepton**. LIMA. Lizard. LOCKER. LOTUS. LUOV. **McNie**. Mersenne-756839. MQDSS. NewHope. NTRUEncrypt. NTRU-HRSS-KEM. NTRU Prime. NTS-KEM. Odd Manhattan. OKCN/AKCN/CNKE. Ouroboros-R. Picnic. pqNTRUSign. pqRSA encryption. pqRSA signature. **pqsigRM**. QC-MDPC KEM. qTESLA. **RaCoSS**. Rainbow. Ramstake. **RankSign**. **RLCE-KEM**. Round2. RQC. **RVB**. SABER. SIKE. SPHINCS+. **SRTPI**. Three Bears. Titanium. **WalnutDSA**.

Some attack scripts already posted causing **total break** or **serious tweaks**. Many more receiving detailed analysis.

Round 1 Candidates

69 accepted as complete, 5 withdrawn within the first 6 months

Family	Signature	Encryption/KEM	Overall
Lattice-based	5	21	26
Code-based	2	17	19
Multivariate	7	2	9
Symmetric-based	3		3
Isogeny-based		1	1
Other	2	4	6
Total	19	45	64

Round 2 Candidates (announced Jan. 30, 2019)

• Encryption/KEMs (17)

- CRYSTALS-KYBER
- FrodoKEM
- LAC
- NewHope
- NTRU (merger of NTRUEncrypt/NTRU-HRSS-KEM)
- NTRU Prime
- Round5 (merger of Hila5/Round2)
- SABER
- Three Bears

9

- BIKE
- Classic McEliece
- HQC
- LEDAcrypt (merger of LEDAkem/pkc)
- NTS-KEM
- ROLLO (merger of LAKE/LOCKER/Ouroboros-R)
- RQC

7

- SIKE

1

- Lattice-based
- Code-based
- Isogenies

▪ Digital Signatures (9)

- CRYSTALS-DILITHIUM
- FALCON
- qTESLA

3

- GeMSS
- LUOV
- MQDSS
- Rainbow

4

- Lattice-based
- Symmetric-based
- Multivariate

- Picnic
- SPHINCS+

2

NIST Report on the 1st Round: <https://doi.org/10.6028/NIST.IR.8240>

Round 3 Candidates (announced July 22, 2020)

FINALISTS	Encryption/KEM	Lattice-based <ul style="list-style-type: none">└ CRYSTALS-KYBER└ NTRU└ SABER	Code-based <ul style="list-style-type: none">└ Classic McEliece
	Digital Signature	Lattice-based <ul style="list-style-type: none">└ CRYSTALS-DILITHIUM└ FALCON	Multivariate <ul style="list-style-type: none">└ Rainbow

ALTERNATE	Encryption/KEM	Lattice-based <ul style="list-style-type: none">└ FrodoKEM└ NTRU Prime	Code-based <ul style="list-style-type: none">└ BIKE└ HQC	Isogeny-based <ul style="list-style-type: none">└ SIKE
	Digital Signature	Symmetric-based <ul style="list-style-type: none">└ Picnic└ SPHINCS+	Multivariate <ul style="list-style-type: none">└ GeMSS	

NSA's Cybersecurity Perspective on PQC

July 29, 2020

- **Strong preference for Lattice-Based Cryptography**
 - “fairly well-studied”
 - “secure when well-parameterized”
 - “among the most efficient”
- **Lattice-based KEM and digital signature scheme to be approved for National Security Systems (NSS)**
- **Stateful signature schemes, LMS and XMSS,**
 - “have a limited number of allowable signatures per key”
 - “require the signer to maintain an internal state”**to be approved for NSS solutions for certain niche applications**
- **NSA CSD does not anticipate the need to approve other PQC schemes for NSS usage**
 - “circumstances could change”

Classical Attack on Rainbow

When: **Feb. 25, 2022**

Who:



Ward Beullens

Postdoc

IBM Research,
Zurich, Switzerland

Time of the attack on 8 cores of
an Intel i9-10885H CPU, running at 2.5 GHz:

Claimed security level 1: **53 hours**

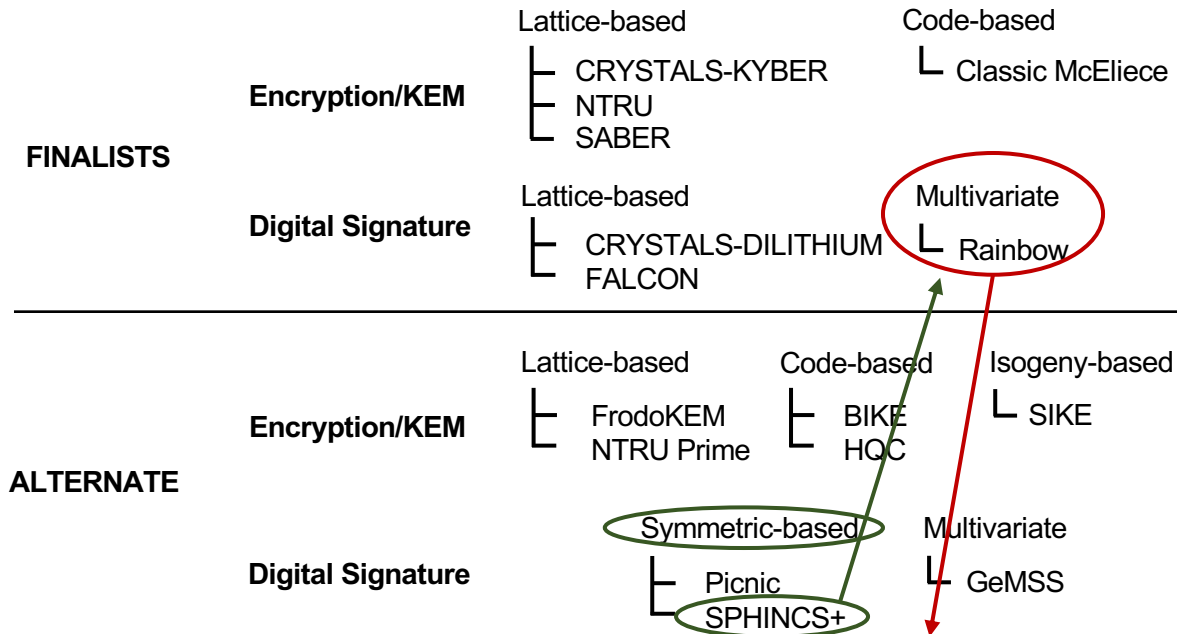
Paper: Cryptology ePrint Archive,
Report 2022/214

Sage Code:

<https://github.com/WardBeullens/BreakingRainbow>

Developments During Round 3

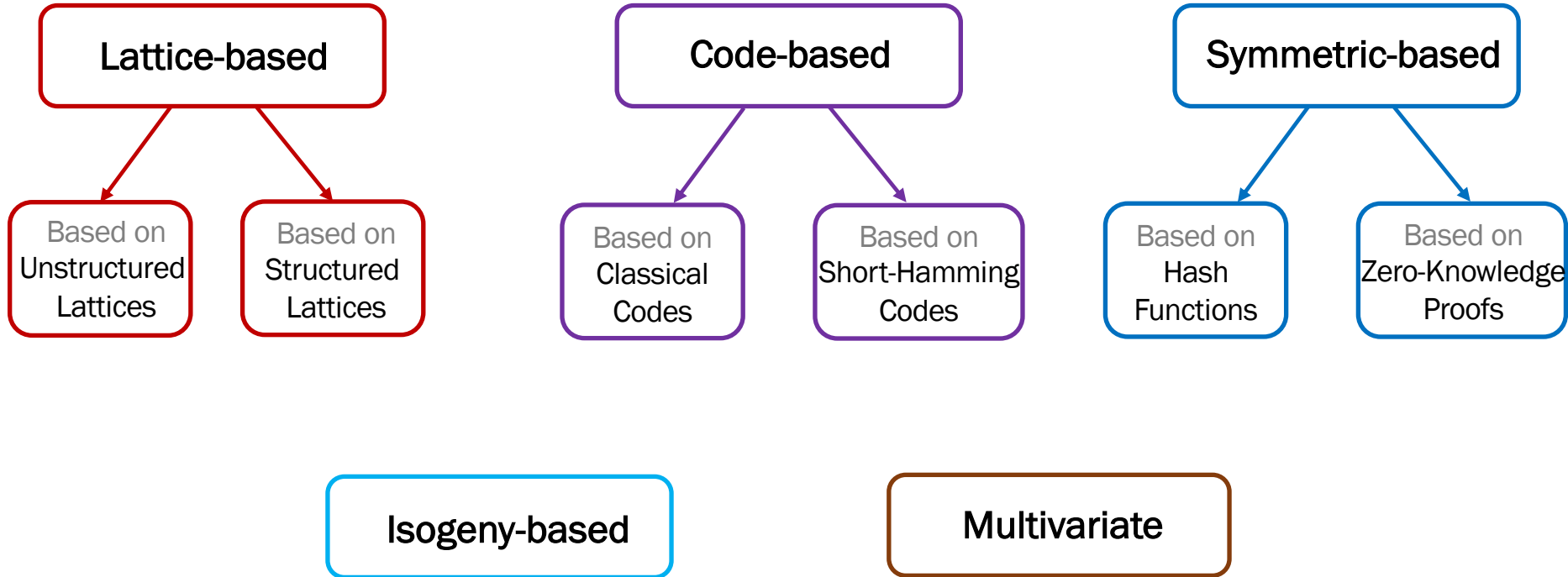
Round 3 Candidates



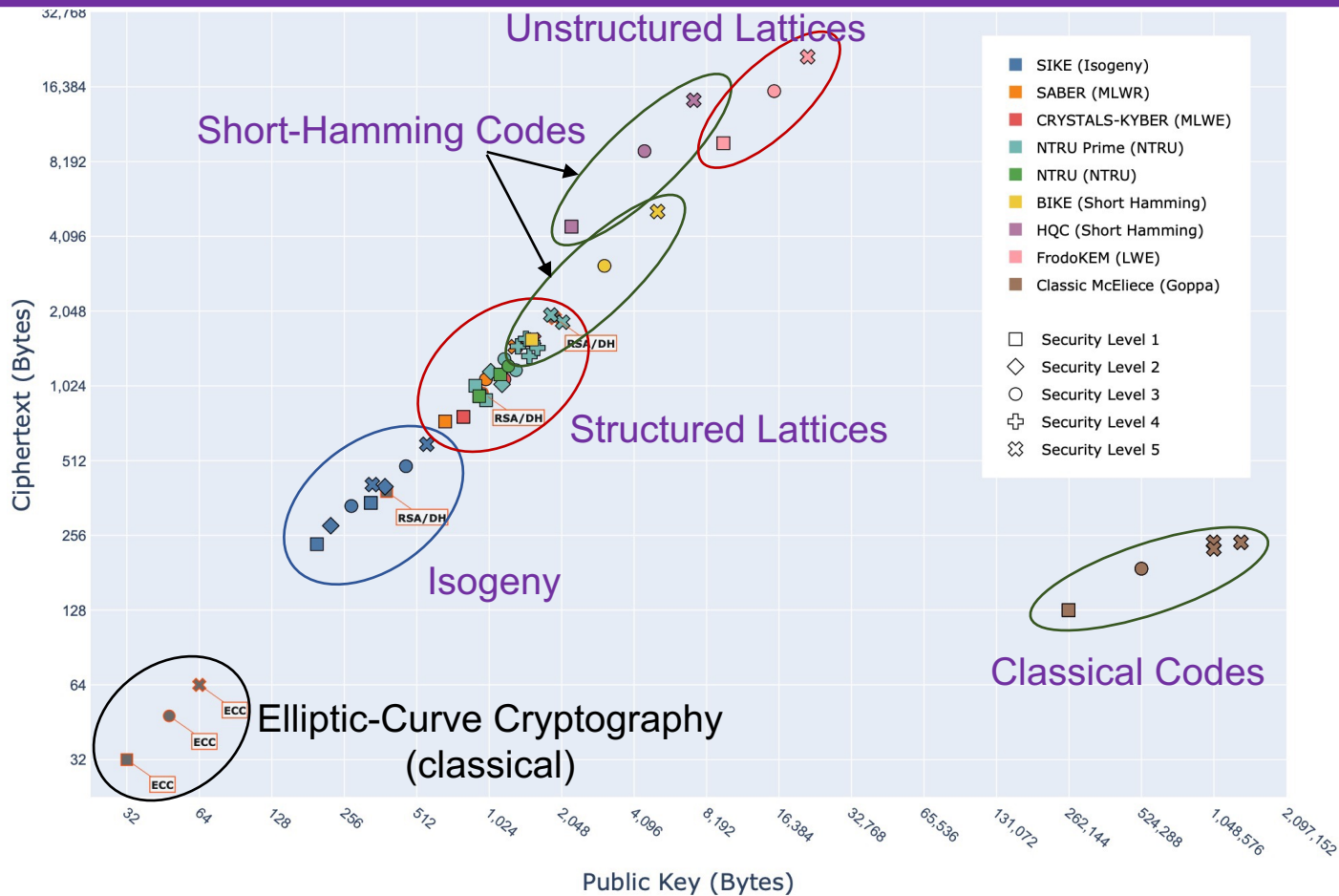
Breaking Rainbow Takes a Weekend on a Laptop

by Ward Beullens, <https://eprint.iacr.org/2022/214>, received 21 Feb 2022

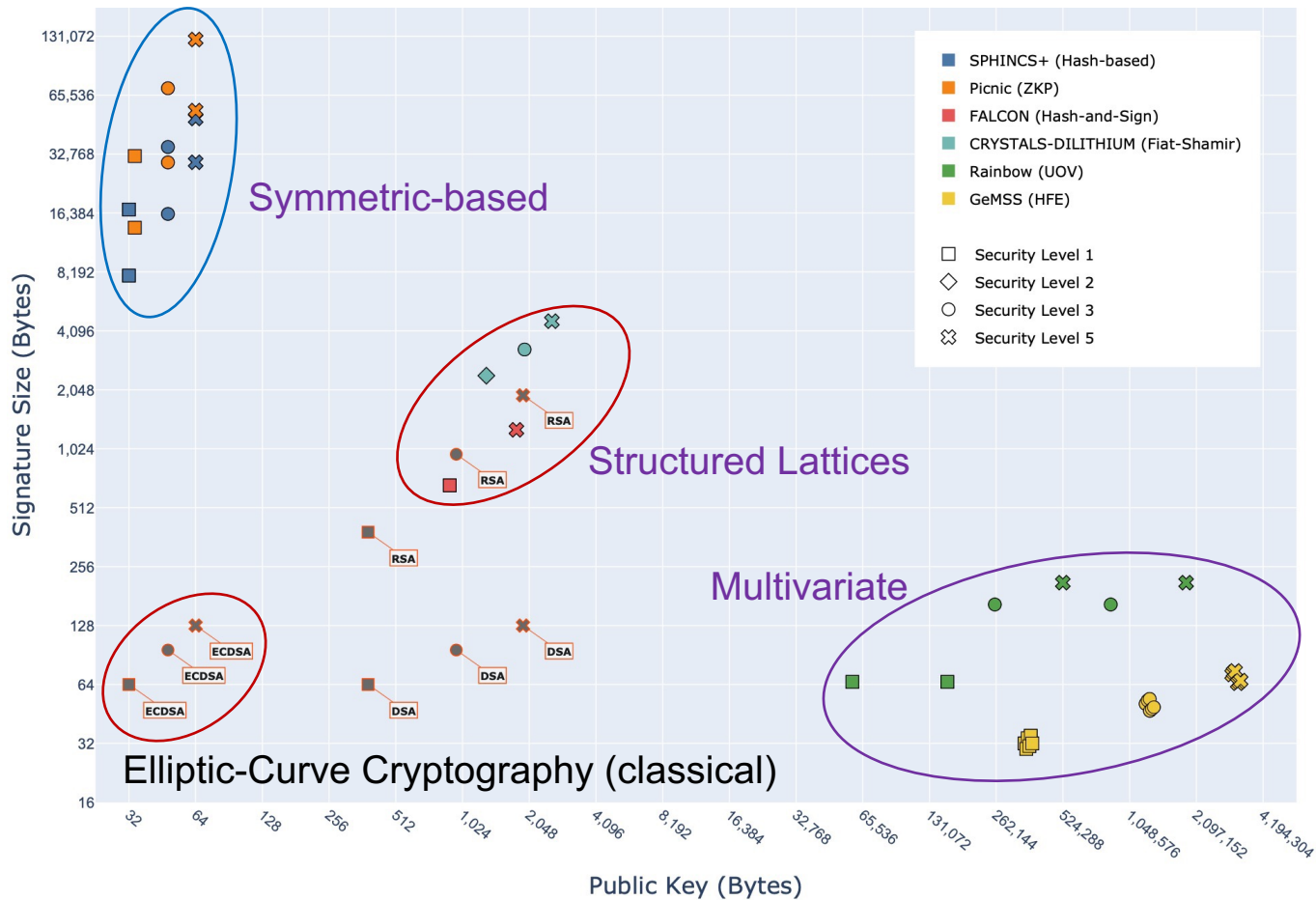
PQC Families and Subfamilies



Round 3 PQC Key Exchange + Classical PKE



Round 3 + Classical Digital Signature Schemes



Favorites for first-generation standards

Key Exchange (Key Encapsulation Mechanism – KEM)

Based on
structured lattices

CRYSTALS-KYBER

SABER

NTRU

Based on
classical codes

Classic McEliece

Digital Signatures

Based on
structured lattices

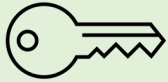
CRYSTALS-DILITHIUM

FALCON

Symmetric-based
(hash-based)

SPHINCS+

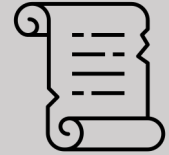
Evaluation Criteria



Size of Keys,
Ciphertext, and
Signatures



Security

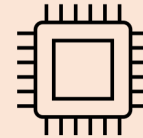


Patent
Issues

Software Efficiency



Hardware Efficiency



Simplicity

Flexibility

Evaluation Criteria – Other Desired Properties

- Drop-in replacements
Compatibility with existing protocols and networks
- Perfect forward secrecy
- Resistance to side-channel attacks
- Misuse resistance
- Ease of implementation (challenging features:
decryption failures, floating-point arithmetic,
Gaussian sampling)

CERG Major Contributions

High-Speed Hardware Implementations of KEMs:

- NTRU (first)
- CRYSTALS-Kyber (fastest)
- Saber (fastest)

Lightweight Hardware Implementations of KEMs Resistant Against Side-Channel Attacks

- Saber (first)

High-Speed Hardware Implementations of Digital Signatures:

- CRYSTALS-Dilithium (2nd fastest)
- Falcon (verification only) (first)

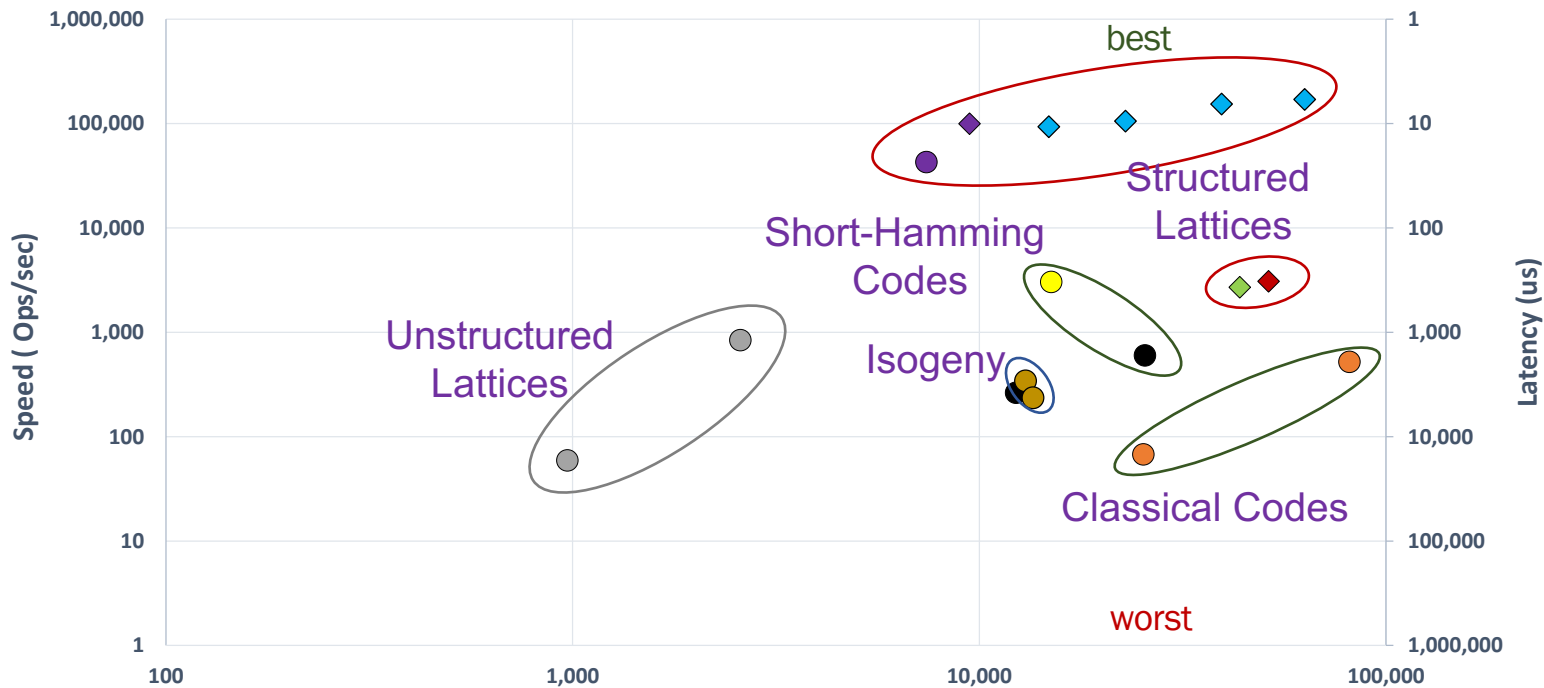
NEON-Based Software Implementations

- NTRU (first)
- CRYSTALS-Kyber (first)
- Saber (first)
- Falcon (first)

Results for KEMs in Hardware

Level 1: Key Generation on Artix-7

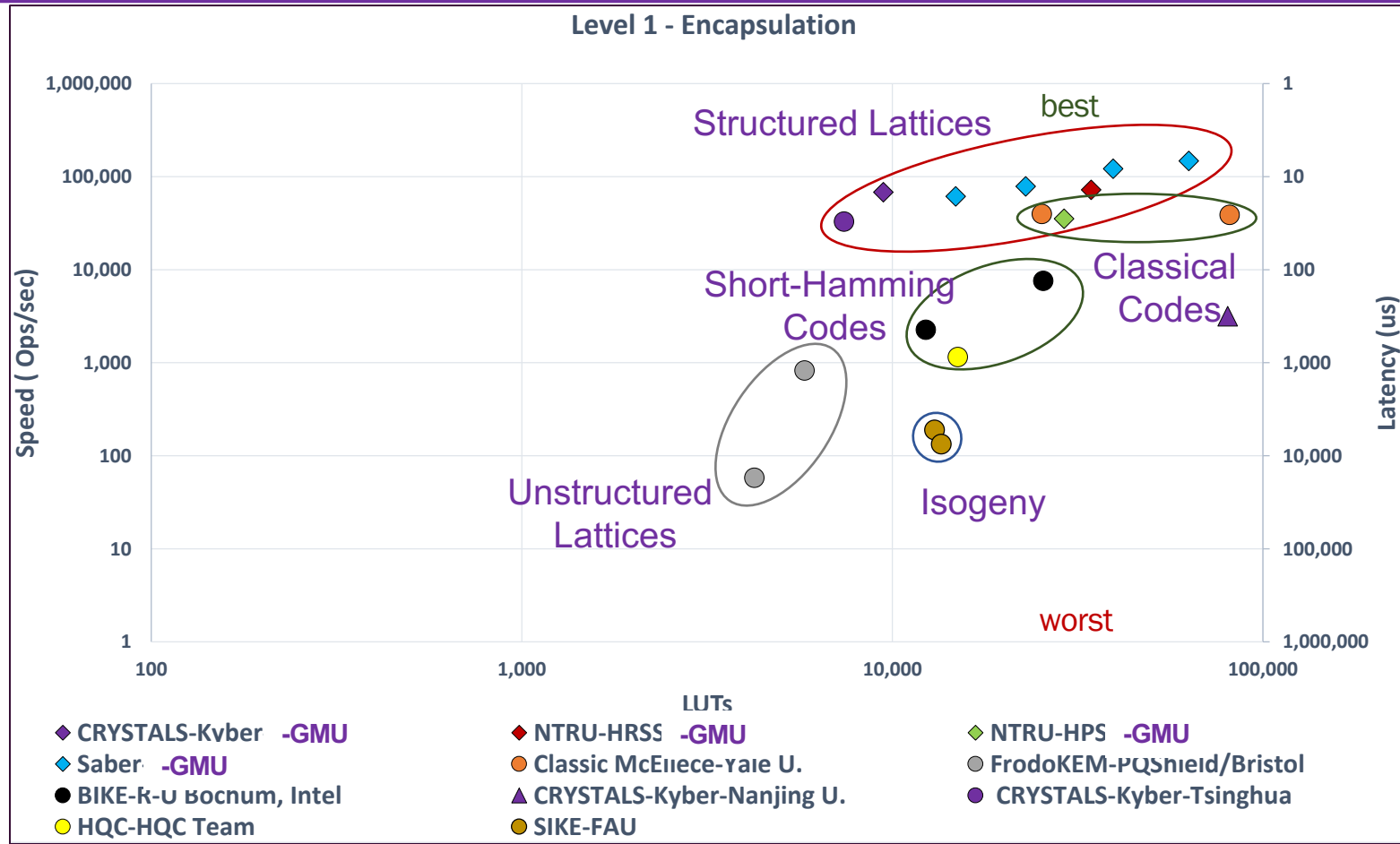
Level 1 - Key Generation



best

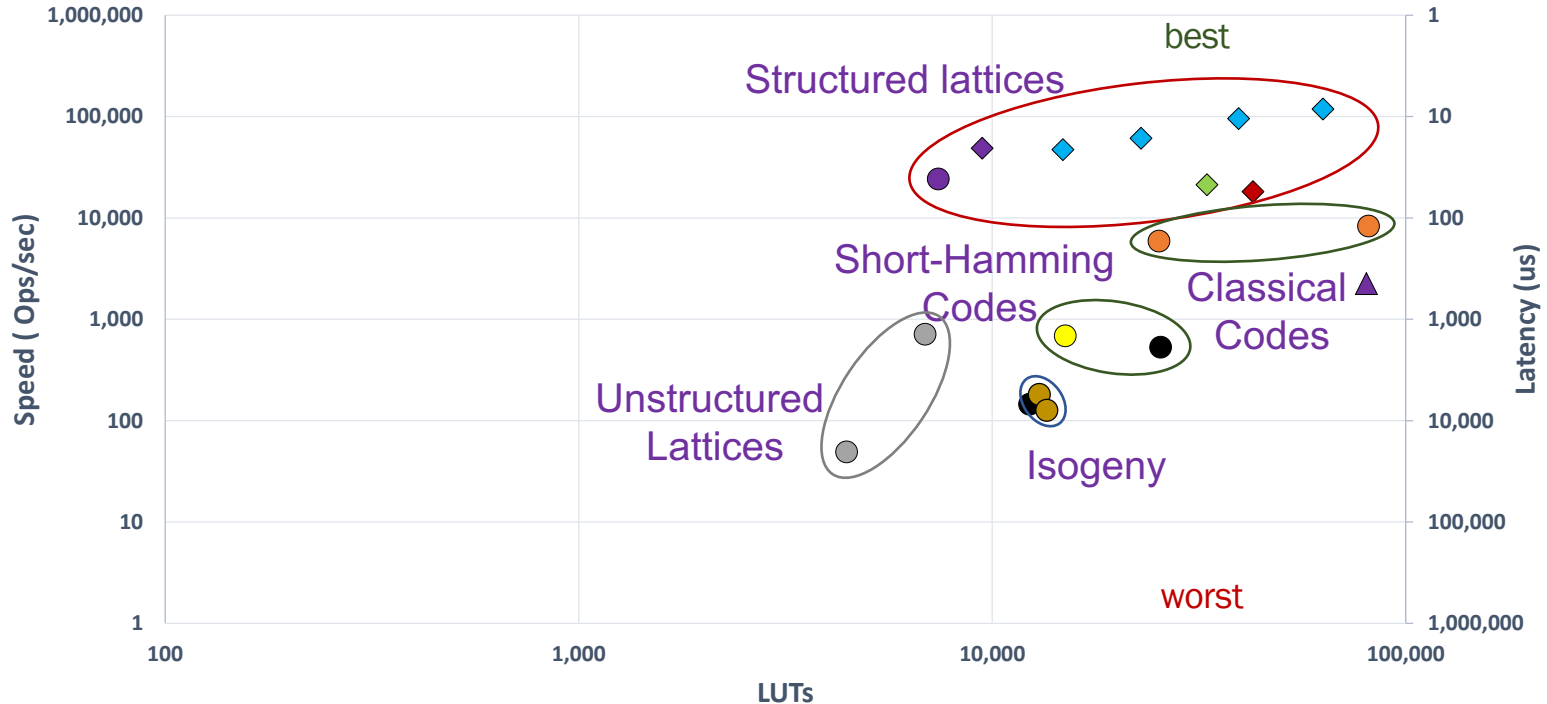
- | | | | |
|----------------------------|-----------------------------|--------------------------|---------------------------|
| ◆ CRYSTALS-Kyber -GMU | ◆ NTRU-HRSS -GMU | ◆ NTRU-HPS -GMU | ◆ Saber -GMU |
| ● Classic McEliece-Yale U. | ● FrodoKEM-PQShield/Bristol | ● BIKE-R-U Bochum, Intel | ● CRYSTALS-Kyber-Tsinghua |
| ● HQC-HQC Team | ● SIKE-FAU | | |

Level 1: Encapsulation on Artix-7



Level 1: Decapsulation on Artix-7

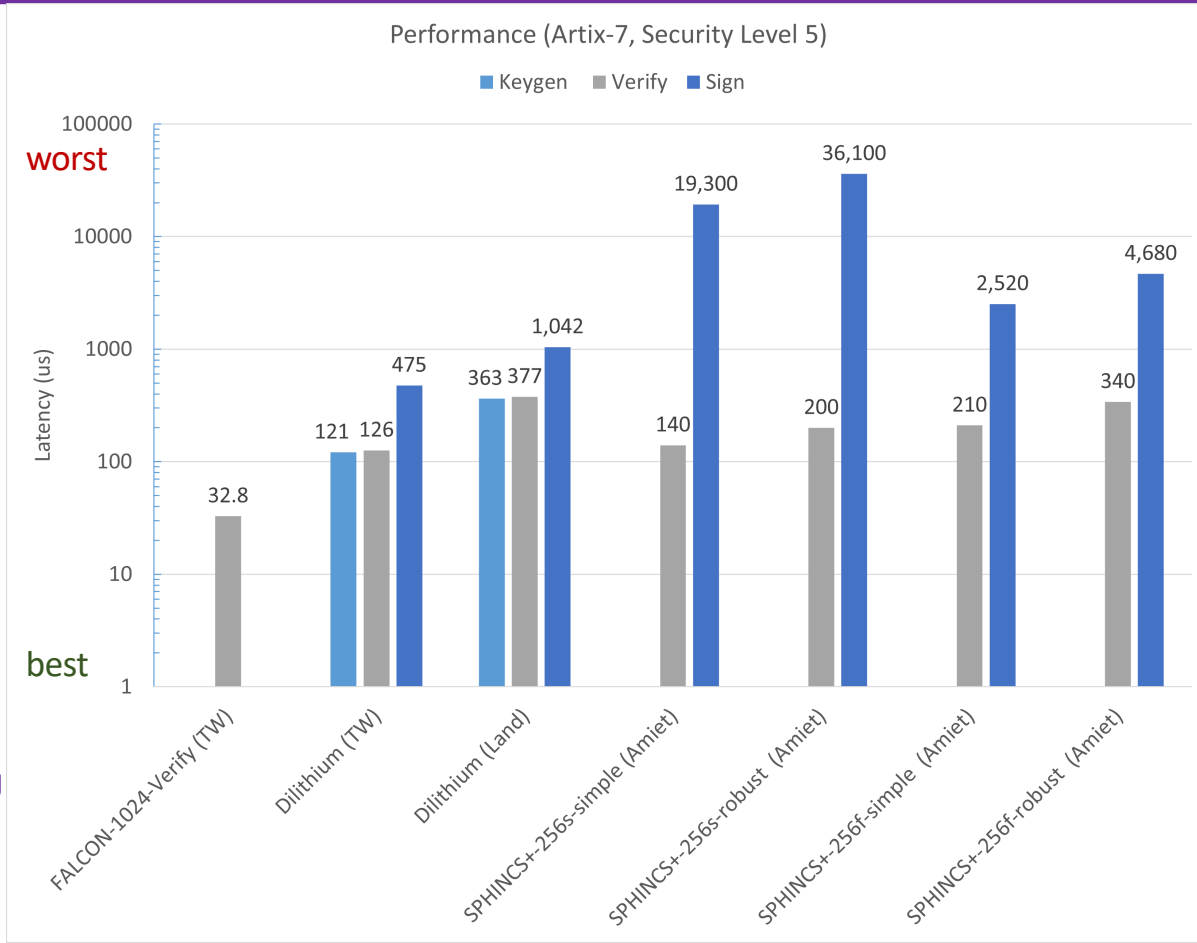
Level 1 - Decapsulation



- ◆ CRYSTALS-Kyber -GMU
- ◆ NTRU-HRSS -GMU
- ◆ NTRU-HPS -GMU
- ◆ Saber -GMU
- Classic McEliece-Yale U.
- FrodoKEM-PQShield/Bristol
- BIKE-R-U B ntel
- ▲ CRYSTALS-Kyber-Nanjing U.
- CRYSTALS-Kyber-Tsinghua
- HQC-HQC Team
- SIKE-FAU

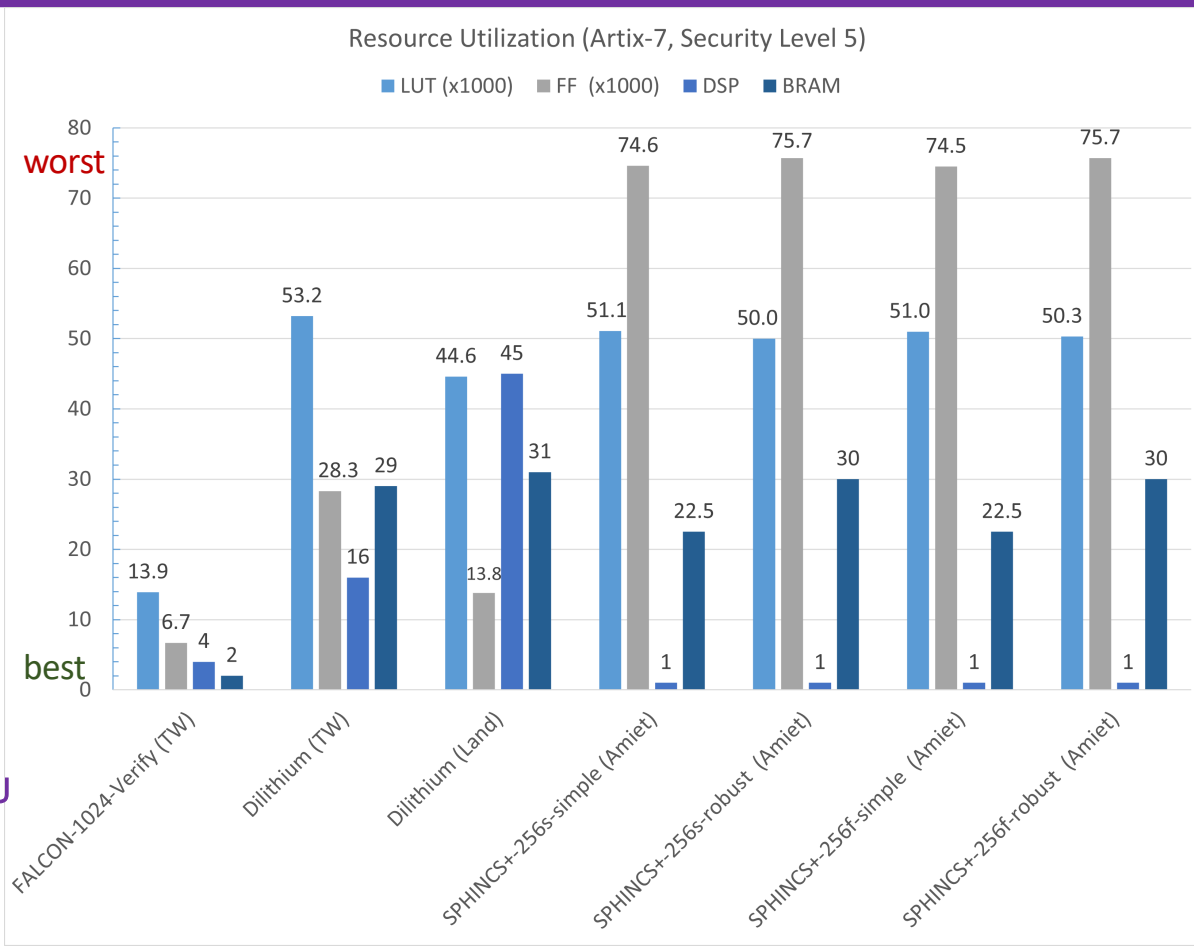
Results for Digital Signatures in Hardware

Level 5: All Operations on Artix-7: Latency



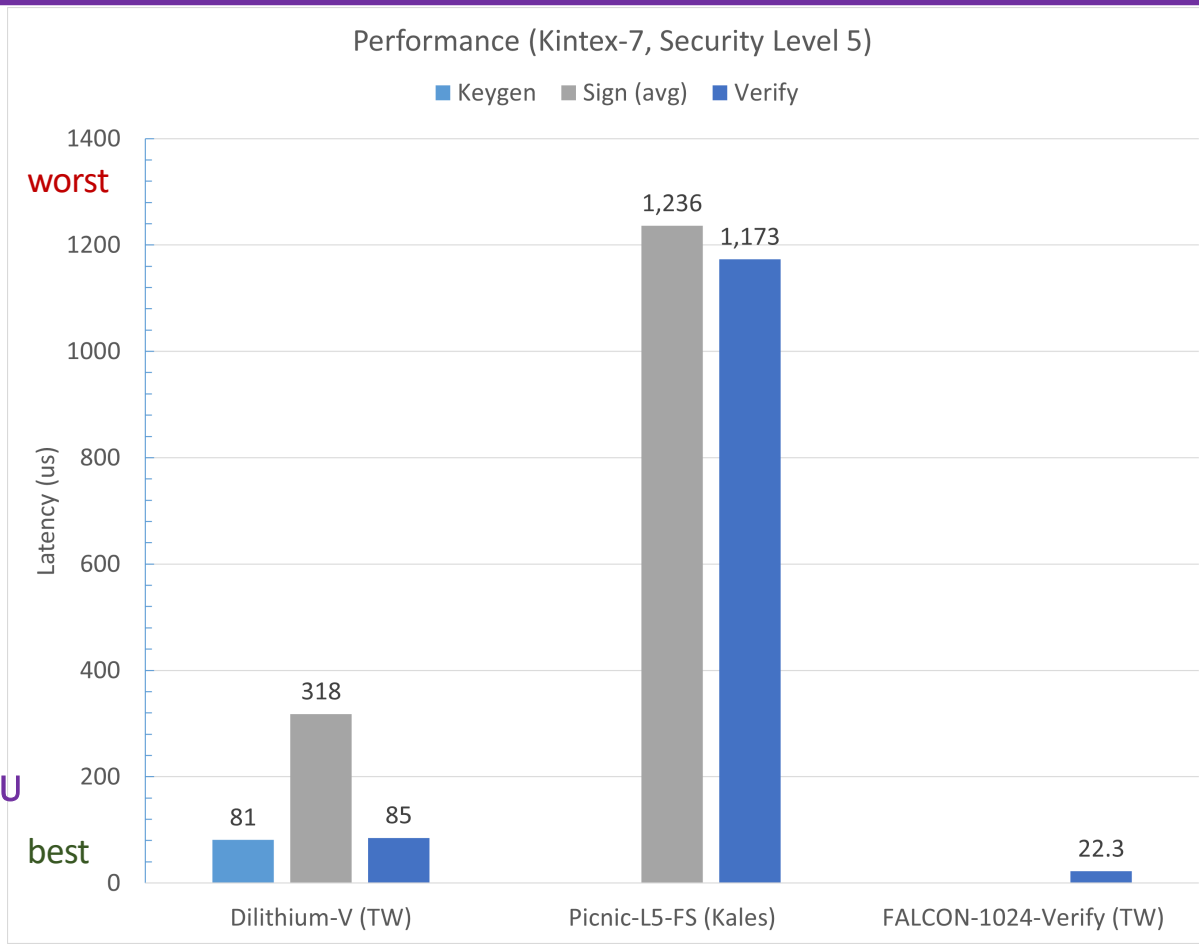
TW- This Work = GMU

Level 5: All Operations on Artix-7: Resource Utilization



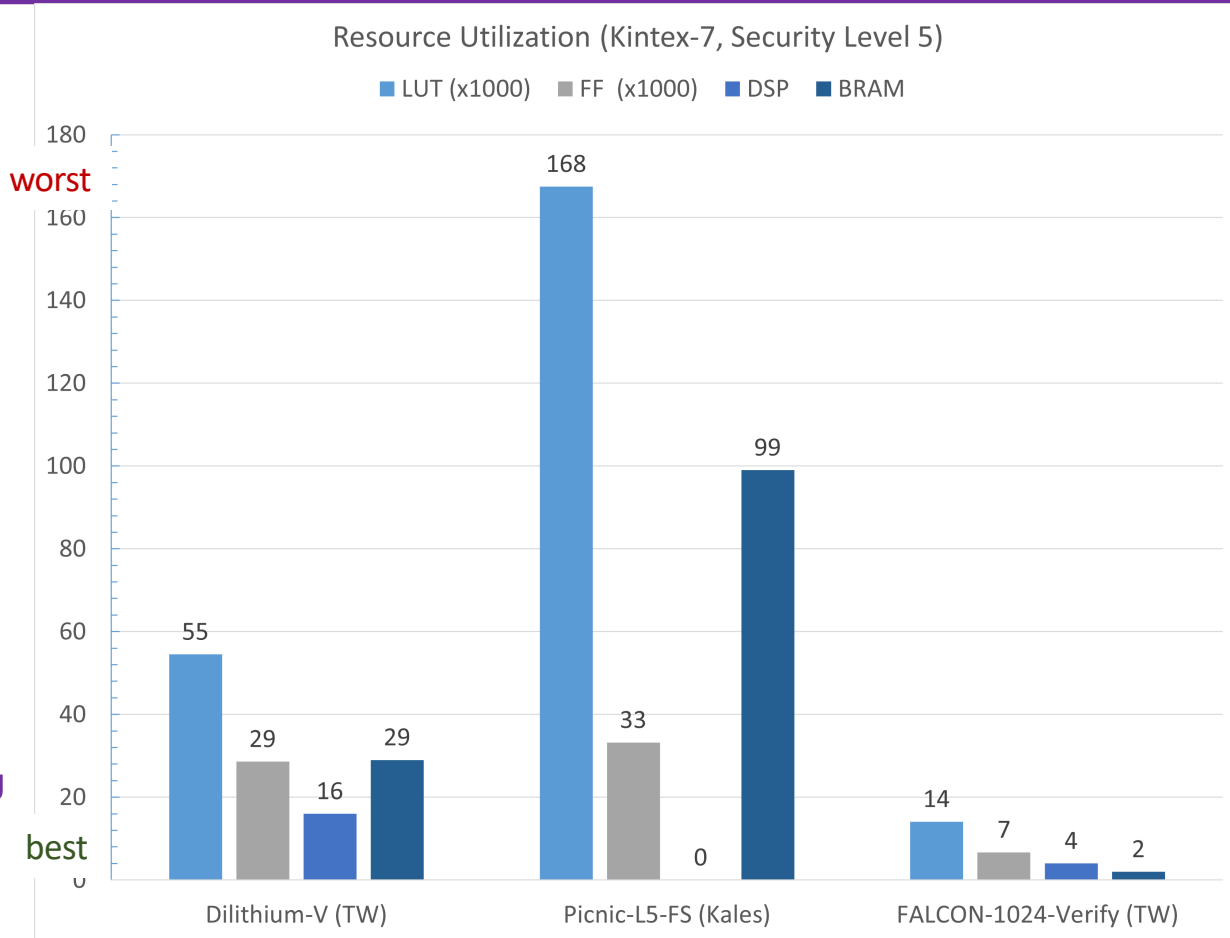
TW- This Work = GMU

Level 5: All Operations on Kintex-7: Latency



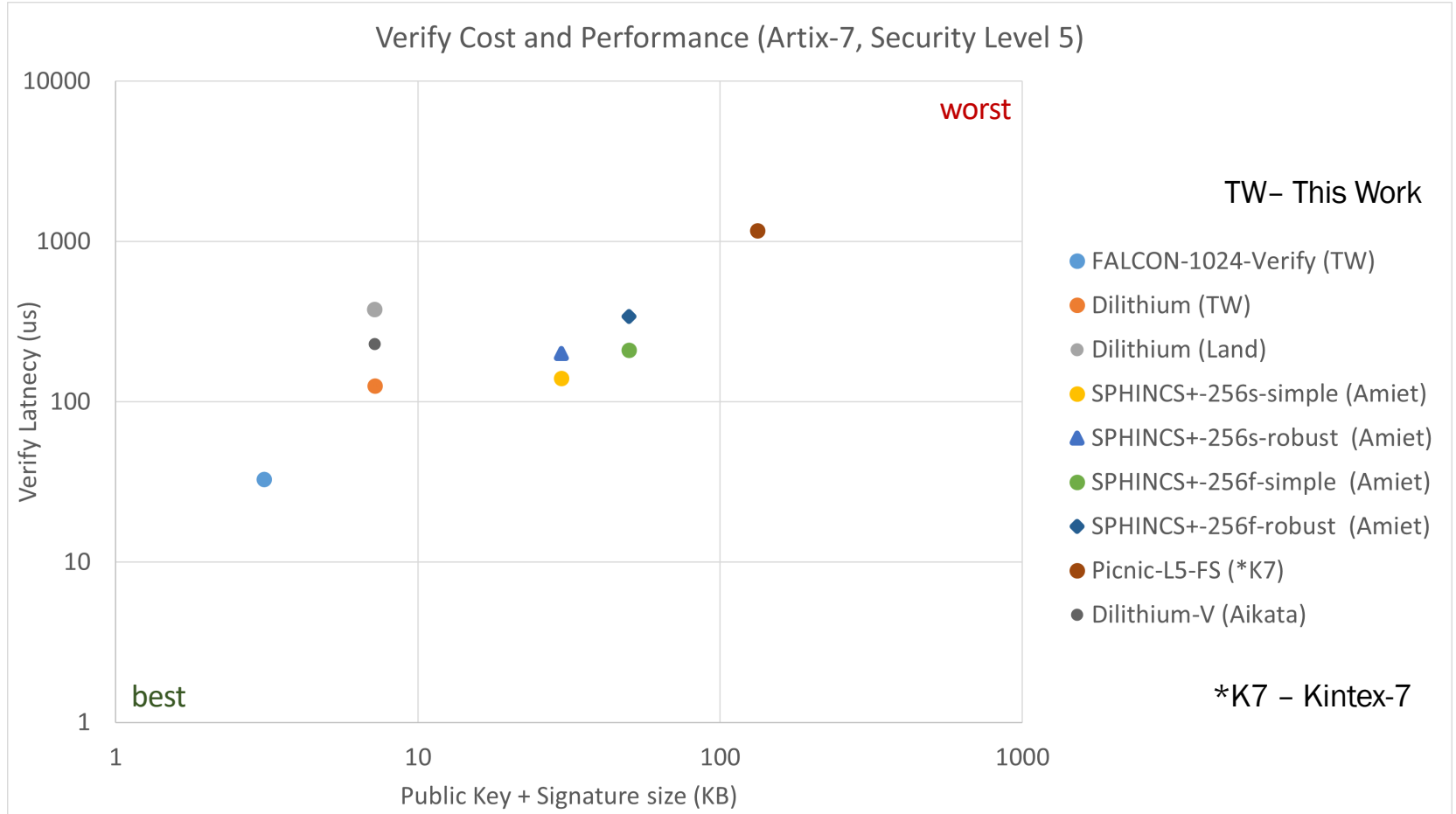
TW- This Work = GMU

Level 5: All Operations on Kintex-7: Resource Utilization



TW- This Work = GMU

Level 5: Signature Verification: Artix-7: Latency vs. Certificate Size

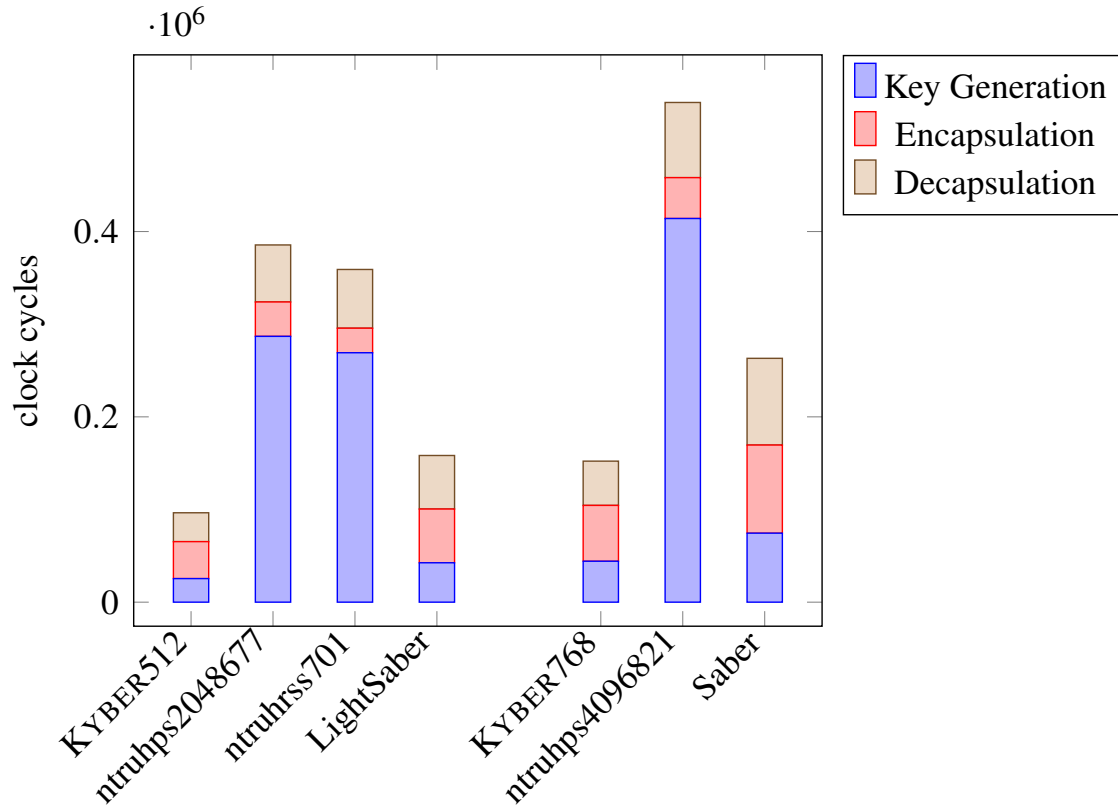


Hardware Benchmarking Summary

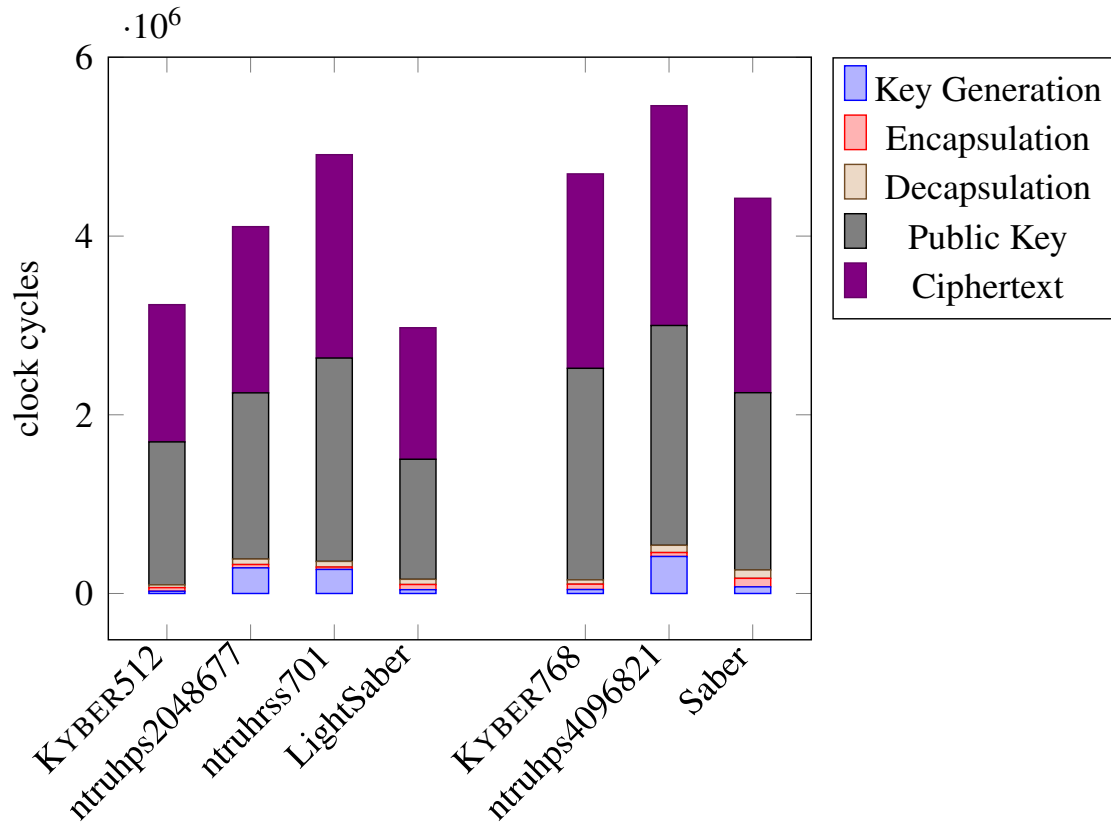
- **High-speed hardware for KEMs:**
 - CRYSTALS-Kyber and Saber comparable; Saber more flexible
 - NTRU and Classic McEliece significantly slower for key generation and somewhat slower for decapsulation and encapsulation
 - SIKE, BIKE, HQC, and FrodoKEM orders of magnitude slower
- **High-speed hardware for Digital Signatures:**
 - CRYSTALS-Dilithium efficient and easy to implement
 - FALCON Verify operation the fastest, but KeyGen and Sign prohibitively complicated
 - SPHINCS+ and Picnic outperformed by CRYSTALS-Dilithium

Software Benchmarking Summary

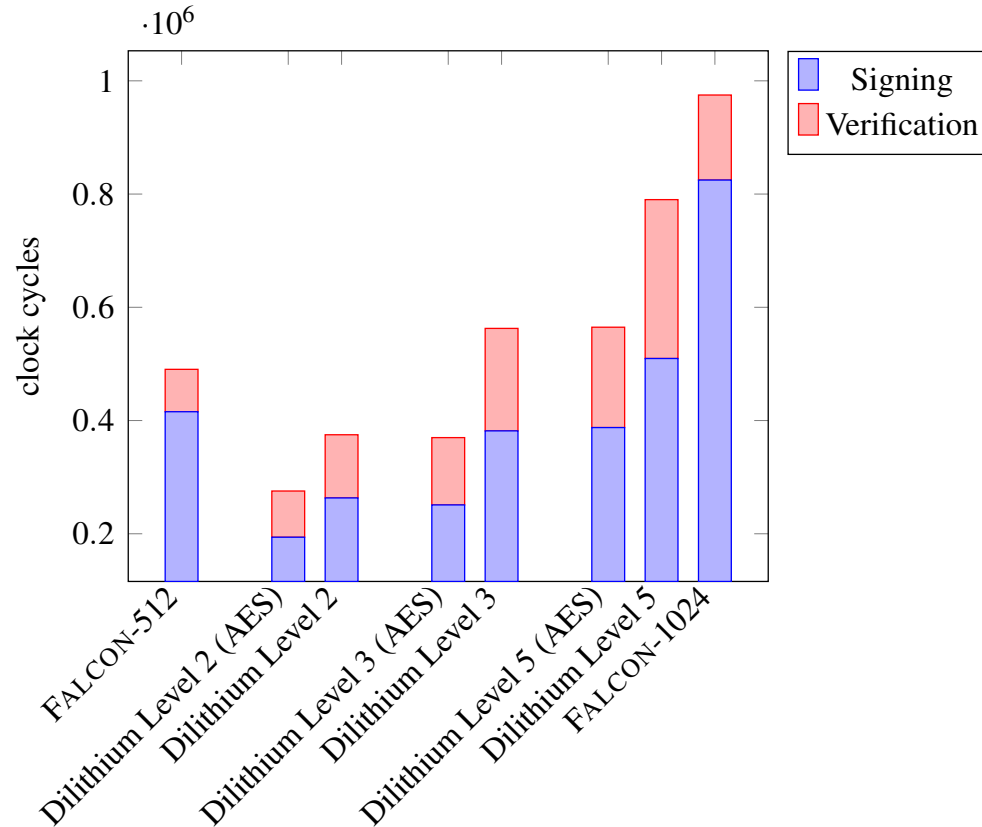
KEM Benchmarks on x86-64 processors with AVX2



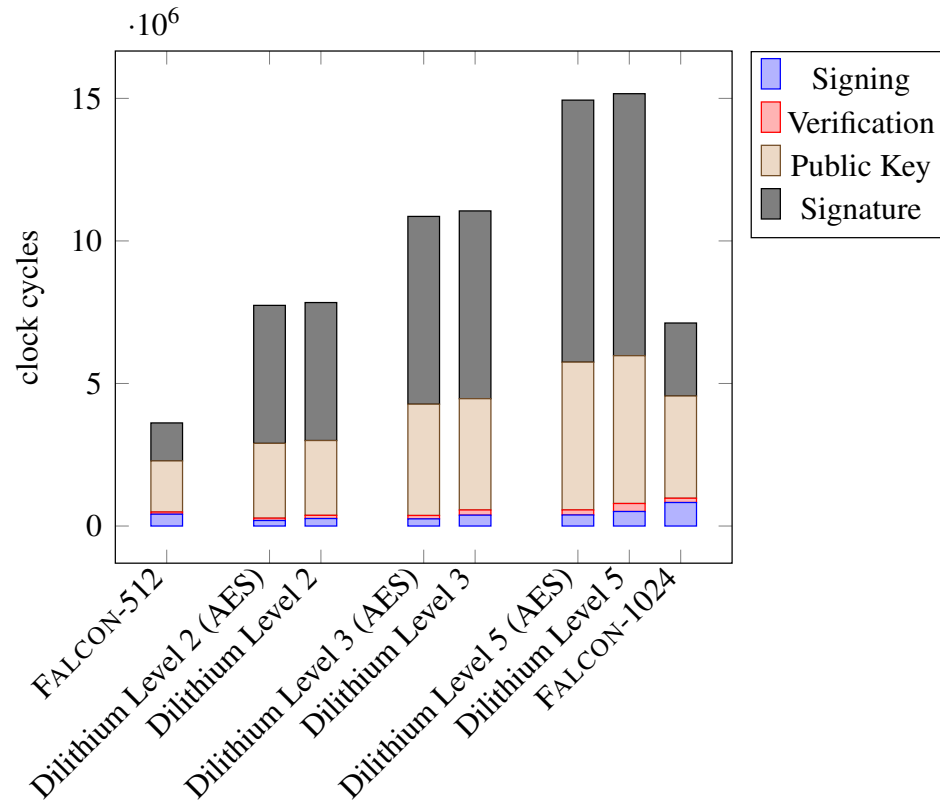
KEM Benchmarks on x86-64 processors with AVX2 with 2000 cycles/byte transmission costs



Digital Signature Benchmarks on x86-64 processors with AVX2



Digital Signature Benchmarks on x86-64 processors with AVX2 with 2000 cycles/byte transmission costs



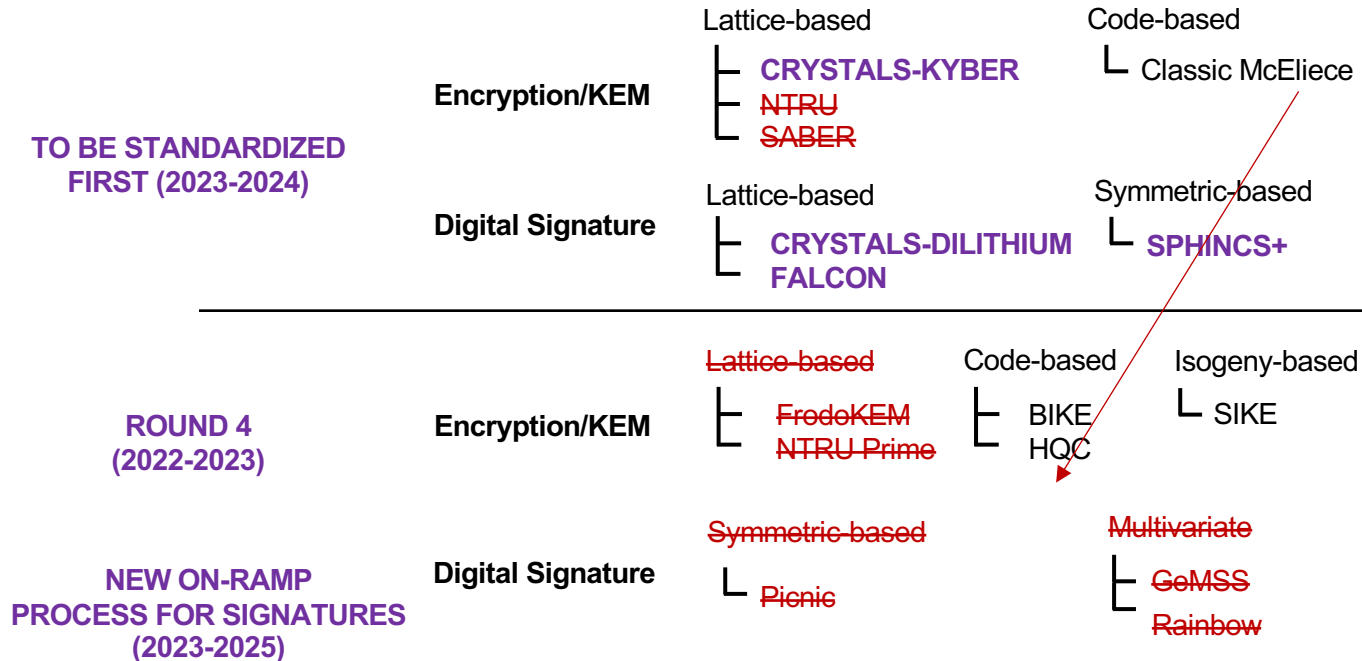
NIST The-end-of-Round 3 Announcement

Before the End of Round 3

Round 3 Candidates

FINALISTS	Encryption/KEM	Lattice-based ┌ CRYSTALS-KYBER ├ NTRU └ SABER	Code-based ┌ Classic McEliece	
	Digital Signature	Lattice-based ┌ CRYSTALS-DILITHIUM └ FALCON	Symmetric-based ┌ SPHINCS+	
ALTERNATE	Encryption/KEM	Lattice-based ┌ FrodoKEM └ NTRU Prime	Code-based ┌ BIKE └ HQC	Isogeny-based ┌ SIKE
	Digital Signature	Symmetric-based ┌ Picnic	Multivariate ┌ GeMSS └ Rainbow	

NIST Decision Published on July 5, 2022



Complete Break of SIKE

Classical Attack on SIKE (1)

When: July 30, 2022

Who:



Wouter Castryck
Research Fellow
COSIC, KU Leuven
2007-present



Thomas Decru
Postdoc
COSIC, KU Leuven
2022-present

Classical Attack on SIKE (2)

Time of the attack using Magma code and Intel Xeon CPU @ 2.60GHz:

SIKEp434 (claimed security level 1):	1 hours 02 minutes
SIKEp503 (claimed security level 2):	2 hours 19 minutes
SIKEp610 (claimed security level 3):	8 hours 15 minutes
SIKEp751 (claimed security level 5):	20 hours 37 minutes

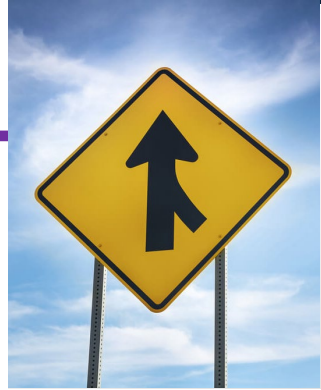
Paper: Cryptology ePrint Archive, Report 2022/975

Magma code: <https://homes.esat.kuleuven.be/~wcastryc>

NIST Call for New Signature Schemes

An On-Ramp for Signatures

Call for Additional Digital Signature Schemes
issued on Sep. 6, 2022; updated in Oct. 2022



- Deadline: **June 1, 2023**
- Main reason: **diversify signature portfolio**
- Candidates on a different track than Round 4 KEMs
- Focus on **general-purpose signatures** that are **not based on structured lattices** (e.g., code-based signatures)
- Schemes with certain unique features may be considered as well, e.g., **schemes with very short signatures**
- The more mature the scheme, the better

Standardization in Other Countries

Countries with Independent Standardization Efforts

Germany:

At the beginning of 2020, the Federal Office for Information Security (BSI) recommended:

- **FrodoKEM** – based on unstructured lattices
- **Classic McEliece** – based on classical codes

China:

The Chinese Association for Cryptologic Research (CACR) held a national cryptographic algorithm design competition in 2018-2019. **79 candidates.**

Winners announced in January 2020:

Digital signatures: **Aigis-sig**

Public-key encryption: **LAC-PKE** and **Aigis-enc**

A blue ribbon graphic with a 3D effect, featuring a darker blue shadow on the left side. The ribbon is horizontal and contains white text.

Transition Plans for National Security Systems

Informal Definition & Recent Developments

Most systems run by the Department of Defense or Intelligence Community fall under the “National Security System” classification.

May 2022:

National Security Memo 10 (NSM-10) signed making it an aim of US to be off quantum vulnerable crypto by 2035

- Calls out to several cybersecurity agencies across the US Government to work in their area of responsibility to ensure a timely transition:
- Calls out NSA to make standards for NSS and give a timeline for deprecation of quantum vulnerable systems

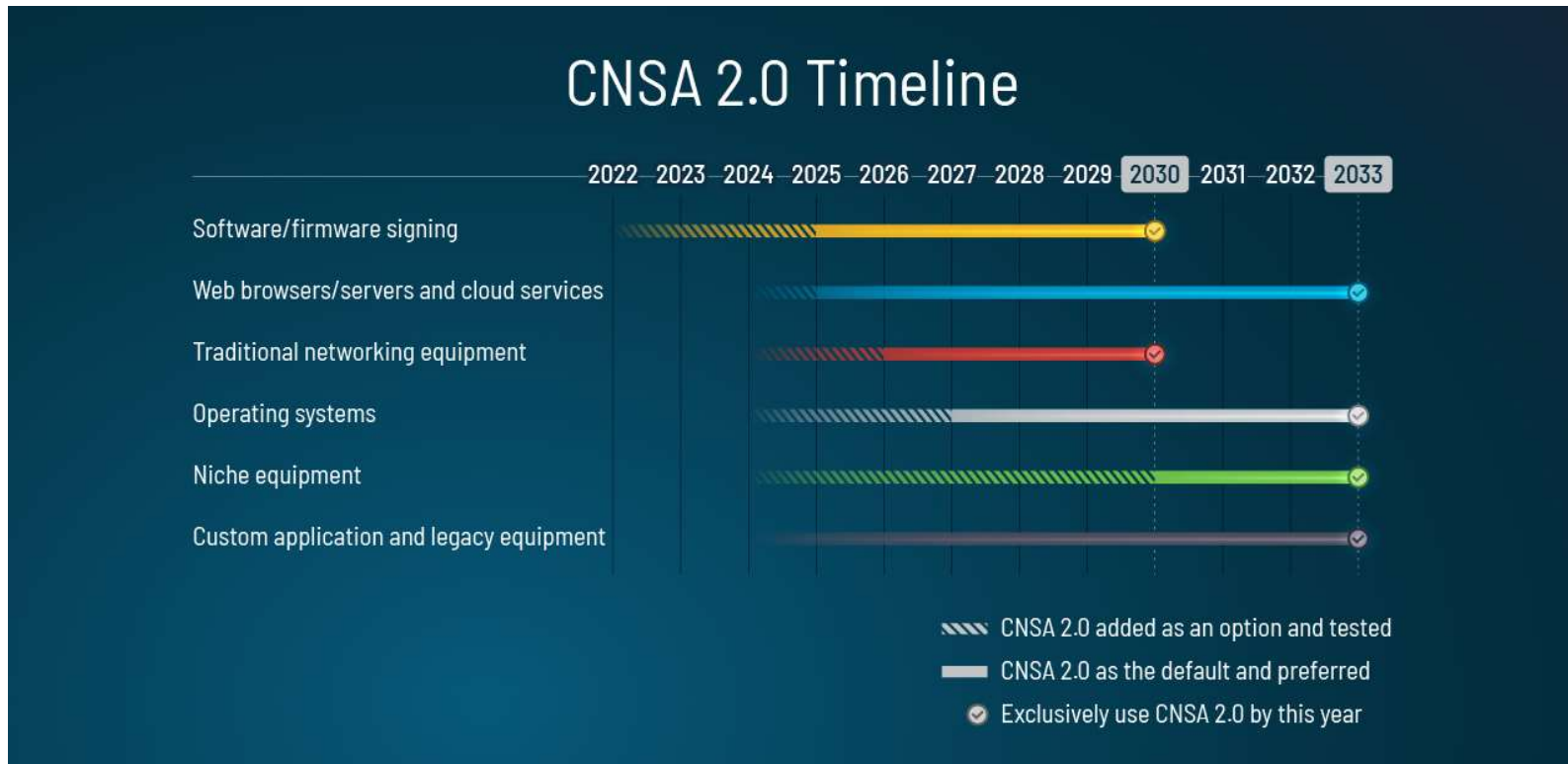
September 2022:

Commercial National Security Algorithm Suite 2.0 (CNSA 2.0) released laying out how to achieve quantum resistance in NSS

Commercial National Security Algorithm (CNSA) 2.0 Suite

Function	Algorithm	Specification
Symmetric block cipher for information protection	AES-256	FIPS 197
Cryptographic hash	SHA-384 or SHA-512	FIPS 180-4
Asymmetric algorithm for key establishment	CRYSTALS-Kyber	TBD
Asymmetric algorithm for digital signature	CRYSTALS-Dilithium	TBD
Asymmetric algorithm for digitally signing firmware and software	Leighton-Micali Signature (LMS) with SHA-256/192, Xtended Merkle Signature Scheme (XMSS)	NIST SP 800-208

CNSA 2.0 Transition Timeline



Source: Morgan Stern (NSA), Transitioning National Security Systems to a Post-Quantum Future, Fourth PQC Standardization Conference, Nov. 29-Dec. 1, 2022

Last Thoughts

PQC Opportunities and Challenges

- The **biggest revolution in cryptography since** the invention of public-key cryptography in **1970s**
- Very **fast changing** field
- A lot of work remaining to be done in terms of **developing new standards** and practical **validation procedures and labs**
- **New candidates** for future standardization still in the pipeline
- **Long and laborious transition period** (easily 10-15 years)
- Many applications require **resistance to side-channel and fault attacks**
- Likely **extensions to Instruction Set Architectures** of multiple major microprocessors
- Excellent **employment opportunities**, especially for U.S. Citizens
- **Start-up and new-product opportunities**

Once in a life-time opportunity! Get involved!

Q&A

Thank You!

Questions?



Comments?

CERG: <http://cryptography.gmu.edu>

ATHENa: <http://cryptography.gmu.edu/athena>

Menu Field: PQC